VES-3600 Advanced Signal Processing

March 7, 2025

Notice

Information in this document is subject to change without notice and does not represent a commitment on the part of Vibrant Technology. Except as otherwise noted, names, companies, and data used in examples, sample outputs, or screen shots, are fictitious and are used solely to illustrate potential applications of the software.

Warranty

Vibrant Technology, Inc. warrants that (a) the software in this product will perform substantially in accordance with the accompanying documentation, for a period of one (1) year from the date of delivery, and that (b) any hardware accompanying the software will be free from defects in materials and workmanship for a period of one (1) year from the date of delivery. During this period, if a defect is reported to Vibrant Technology, replacement software or hardware will be provided to the customer at no cost, excluding delivery charges. Any replacement software will be warranted for the remainder of the original warranty period or thirty (30) days, whichever is longer.

This warranty shall not apply to defects resulting from improper or inadequate maintenance by the customer, customer supplied software or interfacing, unauthorized modification or misuse, operation outside of the environmental specifications for the product, or improper site preparation or maintenance.

If the software does not materially operate as warranted above, the sole remedy of the customer (and the entire liability of Vibrant Technology) shall be the correction or detour of programming errors attributable to Vibrant Technology. The software should not be relied on as the sole basis to solve a problem whose incorrect solution could result in injury to a person or property. If the software is employed in such a manner, it is at the entire risk of the customer, and Vibrant Technology disclaims all liability for such misuse.

NO OTHER WARRANTY IS EXPRESSED OR IMPLIED. VIBRANT TECHNOLOGY SPECIFICALLY MAKES NO WARRANTY OF ANY KIND WITH REGARD TO THIS MATERIAL, INCLUDING, BUT NOT LIMITED TO, THE IMPLIED WARRANTIES OF MERCHANT ABILITY AND FITNESS FOR A PARTICULAR PURPOSE.

THE REMEDIES PROVIDED HEREIN ARE THE CUSTOMER'S SOLE AND EXCLUSIVE REMEDIES. VIBRANT TECHNOLOGY SHALL NOT BE LIABLE FOR ANY DIRECT, INDIRECT, SPECIAL, INCIDENTAL, OR CONSEQUENTIAL DAMAGES IN CONNECTION WITH THE FURNISHING, PERFORMANCE, OR USE OF THIS PRODUCT, WHETHER BASED ON CONTRACT, TORT, OR ANY OTHER LEGAL THEORY.

The software described in this document is copyrighted by Vibrant Technology, Inc. or its suppliers and is protected by United States copyright laws and international treaty provisions. Unauthorized reproduction or distribution of this program, or any portion of it, may result in severe civil and criminal penalties, and will be prosecuted to the maximum extent possible under the law.

You may make copies of the software only for backup or archival purposes. No part of this manual may be reproduced or transmitted in any form or by any means for any purpose without the express written permission of Vibrant Technology.

Copyright © 1992-2025 by Vibrant Technology, Inc. All rights reserved. Printed in the United States of America.

Vibrant Technology, Inc.

13275 East Fremont Place
Suite 200
Centennial, CO 80112 USA

phone: (831) 430-9045

fax: (831) 430-9057

E-mail: support@vibetech.com

http://www.vibetech.com

Table of Contents

VES-3600 Advanced Signal Processing

NOTE: If the **VES-3600 Advanced Signal Processing** option is authorized by your MEscope license, the following commands are enabled in the Data Block (**BLK**) and Shape Table (**SHP**) windows. Execute **Help | License Manager** to verify the Options authorized by your MEscope license.

Additional Data Block (BLK) Commands

- Tools | Integrate
- Tools | Differentiate
- Tools | Remove DC
- Tools | Statistics
- Tools | Histogram
- Tools | Save Statistics
- Tools | Math menu
- Tools | **M#** Matrix menu
- Tools | Data Block Correlation
- Tools | **M#** Pairs Correlation
- Tools | Tachometer Peak Finder
- Tools | Log Decrement
- Tools | M# Envelope

- Transform | Block Size
- Transform | FFT
- Transform | Inverse FFT
- Transform | Window **M#s**
- Transform | Spectra
- Transform | Seed **TRN Chain**
- Transform | **ODS-FRFs**
- Transform | Scale **ODS-FRFs**
- Transform | H1 **FRFs**
- Transform | H2 **FRFs**
- Transform | Outputs
- Transform | Inputs
- Transform | Sinusoidal **ODS**

- Acoustics | A, B, C Weighting
- Acoustics | Narrow to Octave Band
- Acoustics | Calculate Menu
- Acoustics | Intensity to Power
- Acoustics | Acoustic Source Ranking Menu
- Acoustics | Tone Calibration Menu
- Acoustics | Save Ln

Additional Shape Table (SHP) Commands

- Display | Shapes | Acc, Vel, Disp
- Tools | Integrate
- Tools | Differentiate
- Tools | Shape Product
- Tools | Math menu

Additional Data Block (BLK) & Acquisition (ACQ) M#s spreadsheet Columns

- Linear Power
- Input Output
- Peak RMS Pk-Pk
- FFT
- Window, Window Value, Window Correction
- Z-Axis
- Acoustic Weight
- Acoustic Source

Additional Shape Table (SHP) M#s spreadsheet Columns

- Linear Power
- Input Output
- Peak RMS Pk-Pk
- Z-Axis
- Acoustic Weight
- Acoustic Source

Data Block (BLK) M#s Spreadsheet

Linear Power Column

Converts ***all*** (or ***selected***) **M#s** between **Linear** & **Power** engineering units (**EU** & **EU^2**).

- All **M#s** with **Linear** engineering units (**EU**) are converted to **Power** engineering units (**EU^2**), and the measurement values are re-scaled using the formula,

  $$\textbf{Power M\#} = (\textbf{Linear M\#})^2$$

- All **M#s** with **Power** engineering units (**EU^2**) are converted to **Linear** engineering units (**EU**), and the measurement values are re-scaled using the formula,

  $$\textbf{Linear M\#} = \sqrt{\textbf{Power M\#}}$$

Input Output Column

Defines an **M#** as either an **Input, Output**, **Both** or **Cross**.

- A **Cross** channel measurement such as an **FRF** is calculated between two DOFs of a **STR**ucture and is designated as **Cross** in the **Input Output** column of the **M#s** spreadsheet

IMPORTANT: Input, Output, Cross, & Both designations are used by the **Transform** menu commands.

Peak RMS Pk-Pk Column

Scales ***all*** (or ***selected***) **M#s** using the following scale factors.

Amplitude Scaling Choice	M# Is Multiplied By
Peak	1.0
Pk-Pk	2.0
RMS	0.707

FFT Column

Defines the FFT (or DFT spectrum) of each **M#** as either One Sided or Two Sided.

- The FFT calculates a **Two-Sided** spectrum, where ***half*** of a signal is represented by the negative frequency half and ***half*** by the positive frequency half of the spectrum.
- The frequency spectrum of a ***real valued*** time signal is symmetric about zero frequency (DC), so only the ***positive frequency half*** of the spectrum is displayed.
- The ***amplitude*** & ***power*** values for a **One-Sided** FFT are the ***same*** values as its corresponding time domain signal.
- The ***amplitude*** & ***power*** values for a **Two-Sided** FFT are only ***half*** of the values of the original time domain signal.

Window Column

Describes the type of time domain window applied to ***all*** (or ***selected***) **M#s**.

- A Time domain window is applied by executing the **Transform | Window M#s** command.

Window Value Column

Contains the window value corresponding to the **Exponential** or **Force** window listed in the **Window** column.

- The **Exponential** window value is the amount of damping added by the window (in Hz).
- The **Force** window value is the **number of samples** following the beginning of signal where the Force window transitions to zero.

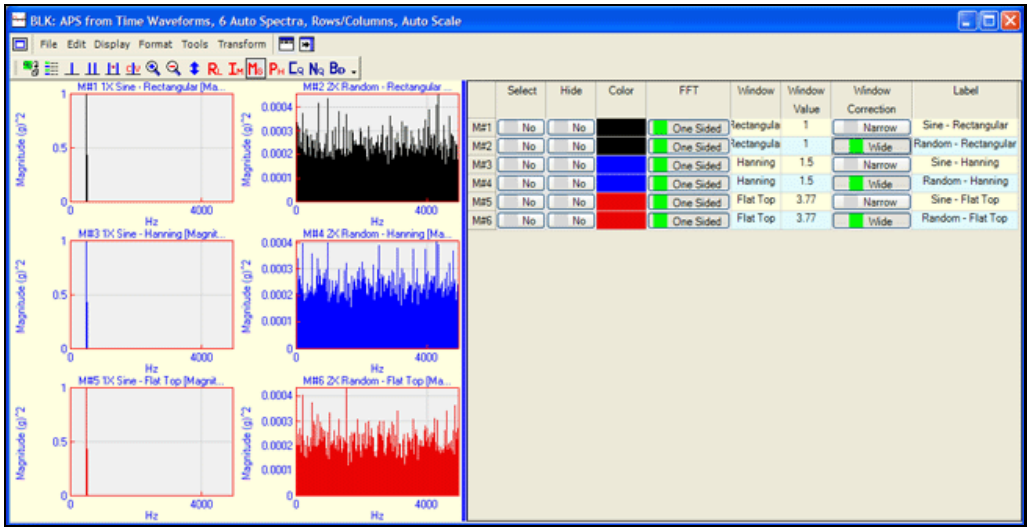
Window Correction Column

Used together with the **Window** & **Window Value columns** to correct the effects of time domain windowed from calculated spectra.

- For each **M#** containing a ***narrow band signal***, choose **Narrow Band** in the **Window Correction** column before applying a time domain window and calculating its spectrum.
- For each **M#** containing a ***wide band signal***, choose **Wide Band** in the **Window Correction** column before applying a time domain window and calculating its spectrum.

Windowing Examples

The figure below contains the spectra of 3 sine wave ***(narrow band)*** signals, and three random ***(wide band)*** signals.

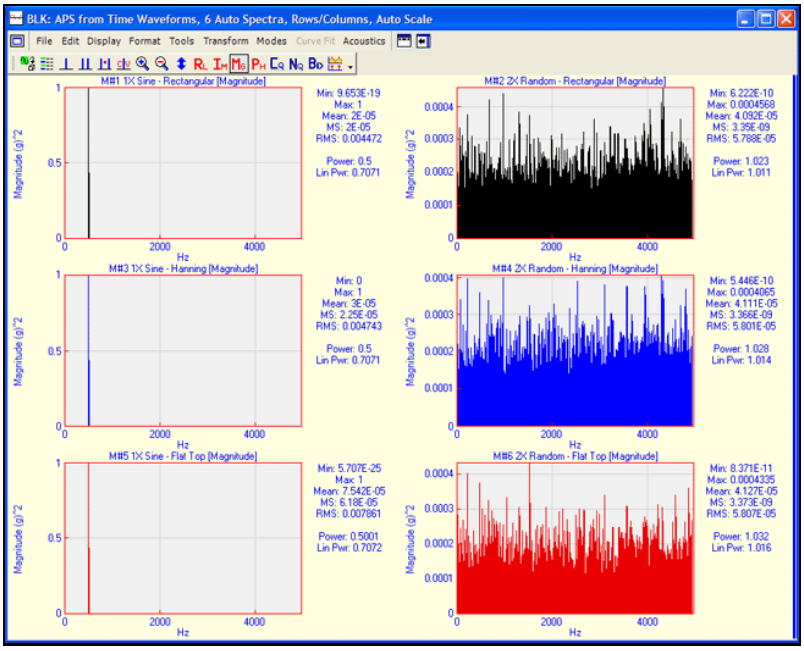


Narrow Band and Wide Band Spectra Amplitude Corrected for Windowing.

- Each **M#** was windowed using **Rectangular**, **Hanning**, and **Flat Top** windows before its Auto spectrum was calculated.
- All the ***magnitudes*** of the **Sine Wave** spectra (on the ***left***) are the same, even though each has been windowed with a different time domain window
- All the ***magnitudes*** of the **Random** spectra (on the ***right***) are ***approximately*** the same, even though each has been windowed with a different time domain window

The figure below shows the Power of 3 sine wave ***(narrow band)*** signals, and three random ***(wide band)*** signals.

- The **Power** in all the **Sine Wave** spectra is the same, since they have been **Narrow Band** corrected
- The **Power** in all the **Random** spectra is the same, since they have been **Wide Band** corrected



Narrow Band and Wide Band Spectra Power Corrected for Windowing.

Z-Axis Column

This column is used to enter a Z-Axis text label for ***all*** (or ***selected***) **M#s.**

- **M#s** can be ***selected*** by their **Z-Axis label** using **M#s | Select | Select By** so that only the shape data from **M#s** with the same **Z-Axis label** is displayed together in animation.

dB Reference Column

Allows you to enter **dB reference values** that are used when **dB** is chosen for the **Y-Axis Scaling** box.

- For **Linear** quantities (such as SPL), dB units are defined as

  Linear dB Units ➔ 20 $\log_{10}$ (magnitude / dB Reference value)

- For **Power** quantities (such as Sound Power & Intensity), dB units are defined as

  Power dB Units ➔ 10 $\log_{10}$ (magnitude / dB Reference Value)

Acoustic Weight Column

Indicates the type of acoustic weighting (A, B, C) applied to each **M#**.

Acoustic Source Column

Used to enter a **text name** for each **M#** belonging to an acoustic source.

Data Block (BLK) Display Menu

M#s | Display | Real

Displays either **real M#** data, or the **real part of complex M# data** in **Octave** band and/or **dB** units.

*Data Block (**BLK**) Window Showing Real Part of Octave Data.*

Octave Band Data

- **Log** or **dB** formats can be chosen for displaying the Real part of Octave band data
- **Linear, Log, dB** & **decades** choices are made in the **Format | Y-Axis** dialog box
- ***Right click*** in the **M#** graphics area and execute **Format | Y-Axis** from the menu to open the Y-Axis dialog box

Real Part in dB Reference Units

- The Real part is displayed in dB units relative to a reference level if a reference level is entered in the **dB Reference column** in the **M#s** spreadsheet

- For **Linear (RMS)** data, the Real part is displayed as

  Real part (dB Reference) = Sign (Real part) [20 Log $_{10}$ (Abs (Real part) / Linear Reference)]

- For **Power (MS)** data, the Real part is displayed as

  Real part (dB Reference) = Sign (Real part) [10 Log $_{10}$ (Abs (Real part) / Power Reference)]

M#s | Display | Magnitude

Displays the magnitude of the measurement data in **Octave** band and/or **dB** units.

*Data Block (**BLK**) Window Showing Log Magnitude of Octave Data.*

Linear, Log or dB

Magnitudes can be displayed in **Linear, Log** or **dB** format.

- When **Log** or **dB** is chosen, you can also choose **1** to **14** decades (powers of 10) to display
- **Linear, Log, dB** & **decades** choices are made in the **Format | Y-Axis** dialog box
- ***Right click*** in the **M#** graphics area and execute **Format | Y-Axis** from the menu to open the **Y-Axis** dialog box

dB Units for Linear Versus Power Quantities

Magnitudes can be displayed in dB (decibel) units.

- For **Linear** (RMS) quantities, (such as **FRFs**, Linear Spectra, etc.) the Magnitude is displayed as,

  Magnitude (dB) = 20 Log $_{10}$ (Magnitude)

- For **Power** (MS) quantities, (such as Auto Power Spectra, PSDs, etc.), the Magnitude is displayed as,

  Magnitude (dB) = 10 Log $_{10}$ (Magnitude)

Magnitude in dB Reference Units

Magnitudes can also be displayed in dB (decibel) units relative to a reference level.

- For **Linear (RMS)** quantities, (such as SPL) the Magnitude is displayed as,

  Magnitude (dB Reference) = 20 Log $_{10}$ (Magnitude / Linear Reference)

- For **Power (MS)** quantities, (such as Sound Power & Intensity), the Magnitude is displayed as,

  Magnitude (dB Reference) = 10 Log $_{10}$ (Magnitude / Power Reference)

- To display magnitudes in **dB Reference** units, the **Linear (RMS) Reference** or **Power (MS) Reference** values must be entered in the **dB Reference** column in the **M#s** spreadsheet
  - A Linear (RMS) Reference value is required for Linear (RMS) M# data
  - A Power (MS) Reference value is required for Power (MS) M# data

Data Block (BLK) Tools Menu

Tools | Integrate

Performs Integration on ***all*** (or ***selected***) **M#s** in a Data Block (**BLK**).

- All integration is done in the frequency domain
- Time domain waveforms are transformed to the frequency domain, integrated, and transformed back to the time domain.
- Frequency domain **M#s** are integrated by ***dividing the spectrum by frequency***,

$$\int x(t)dt \Leftrightarrow \frac{X_i(2\pi f_i)}{j2\pi f_i}$$

x(t) = continuous **TWF**

$X_i(2\pi f_i)$ = linear spectrum (**DFT**) of the signal for the **i^{th}** sample

$2\pi f_i$ = frequency of the **i^{th}** sample (**radians/second**)

f_i = frequency of the **i^{th}** sample (**Hz**)

j = the imaginary operator

Integration Errors Due to DC Offset

If a time domain waveform has any **DC Offset (or bias)** in it, integration of the DC Offset will result in a ***ramp function***.

- To ***minimize errors*** due to any DC Offset, **Tools | Remove DC** is ***automatically executed*** before integration is performed

Integration Errors Due to Leakage

The FFT assumes that the signals to be transforming are ***periodic,*** or ***completely contained*** within their ***sampling window***. The ***sampling window*** is the range of samples in each **M#**.

- If a time domain waveform is ***non-periodic,*** or ***not completely contained*** within its ***sampling window***, ***smearing*** (called ***leakage***) of its spectrum will occur when it is transformed to the frequency domain
- If a frequency spectrum is ***non-periodic,*** or ***not completely contained*** within its ***sampling window***, leakage (called ***wrap around error***) of its **TWF** will occur when it is transformed to the time domain

Removing Lower Frequencies Before Integration

Integration ***amplifies*** the ***lower frequencies*** in a signal

- To reduce the harmful effects of all ***non-essential*** lower frequencies in a signal, they should be removed from its spectrum ***before integrating it***.
  - Execute **Transform | FFT** to transform time domain waveforms to the frequency domain
  - Set up the **Band cursor** to include all non-essential low frequencies
  - Execute **Transform | Window M#s** and apply the **Notch** window to remove the low frequencies (***zero*** the **M#** values)
  - Execute **Tools| Integrate** to integrate the **M#s**
  - Execute **Transform | Inverse FFT** to transform the integrated signals back to the time domain

Tools | Differentiate

Performs differentiation on ***all*** (or ***selected***) **M#s** in a Data Block (**BLK**).

- All differentiation is done in the frequency domain
- Time domain waveforms are transformed to the frequency domain, differentiated, and transformed back to the time domain
- Frequency domain **M#s** are differentiated by ***multiplying the spectrum by frequency***,

$$\frac{d\big(x(t)\big)}{dt} \Leftrightarrow j2\pi f_i\big(X_i(2\pi f_i)\big)$$

x(t) = continuous **TWF**

$\mathbf{X_i(2\pi f_i)}$ = linear spectrum (**DFT**) of the signal for the $\mathbf{i^{th}}$ sample

$\mathbf{2\pi f_i}$ = frequency of the $\mathbf{i^{th}}$ sample (**radians/second**)

$\mathbf{f_i}$ = frequency of the $\mathbf{i^{th}}$ sample (**Hz**)

j = the imaginary operator

Tools | Remove DC

Removes the DC offset (or bias) from ***all*** (or ***selected***) **M#s** in a Data Block (**BLK**).

- The following steps are carried out on time domain waveforms,
  - Execute **Transform | FFT** to transform all **M#s** to the frequency domain
  - Zero the DC component (at frequency = 0) of the spectrum
  - Execute **Transform | Inverse FFT** to transform all **M#s** back to the time domain

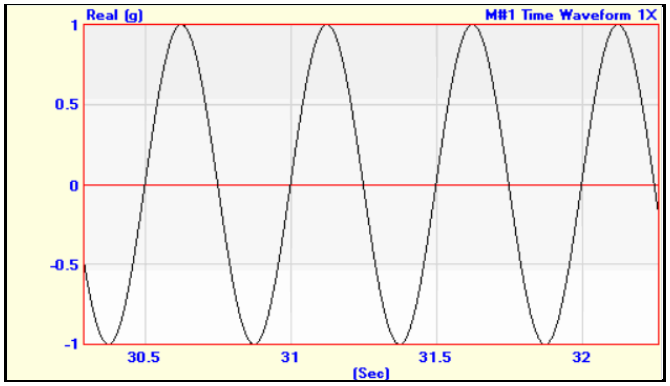
Tools | Histogram

Calculates a Histogram (or **Normal Distribution**), and its **Cumulative Distribution** of the Y-Axis values in a Data Block (**BLK**).

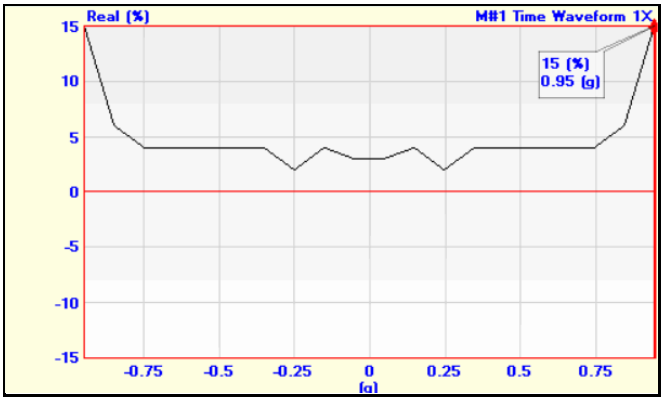
- A Histogram is a **count** of the number of Y-axis values that lie between two values, referred to as a "**bin**"
- The Y-Axis of the Histogram is displayed as a **percentage** of the total number of values in all bins
- The X-Axis of the Histogram is the limits of the Y-Axis values in the Data Block (**BLK**) divided by the number of bins
  - If the **Band** cursor is displayed, the Histogram of the data in the band is calculated
  - If the data display is **Zoomed**, the Histogram of the Zoomed data is calculated

- If the **Real** part, **Imaginary** part, or **Phase** of complex data is displayed, the Histogram of that data is calculated.
- Otherwise, the Histogram of the **Magnitude** is calculated

The figure below shows a **sine wave M# with 10000 samples** followed by its Histogram using 20 bins.

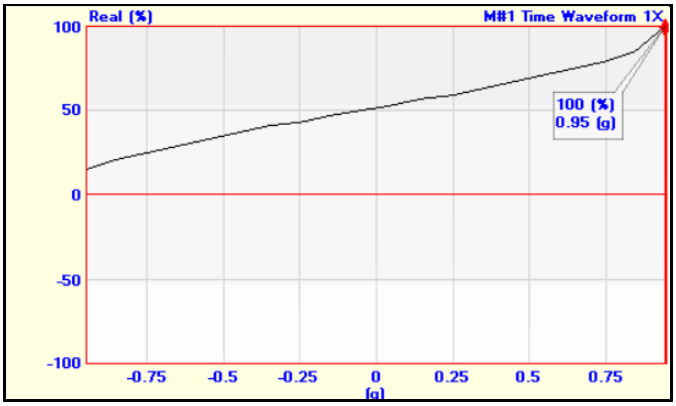


10000 Samples of a Sine Wave.



Histogram of the Sine Wave using 20 Bins.

The figure below shows the **Cumulative Distribution** of the **sine wave M# with 10000 samples** using a Histogram with 20 bins.

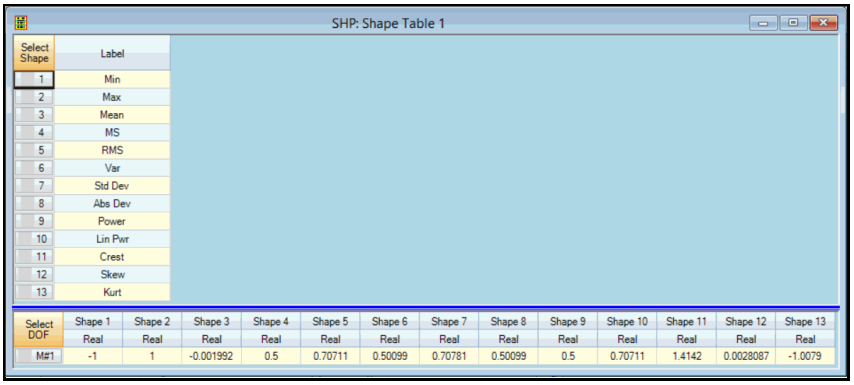


Cumulative Distribution of the Sine Wave using 20 Bins.

Tools | Save Statistics

Saves the statistics of each measurement (**M#**) in a Data Block (**BLK**) into a Shape Table (**SHP**).

- Each statistic is saved as a different shape
- Each shape **M#** is the statistics value for the ***corresponding M#*** in the Data Block (**BLK**)
- If the **Band** cursor is displayed, the statistics only for data in the band are saved
- If the data display is **Zoomed**, the statistics only for the displayed data are saved
- If the **Real** part, **Imaginary** part, or **Phase** of complex data is displayed, the statistics for that data are saved
  - Otherwise, the statistics of the Magnitude are saved

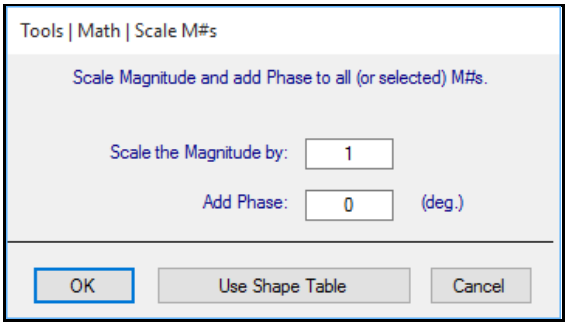


*Data Block (**BLK**) Statistics Saved in a Shape Table (**SHP**).*

Tools | Math | Scale M#s

Multiplies ***all*** (or ***selected***) **M#s** by a ***magnitude*** and ***adds phase*** to them.

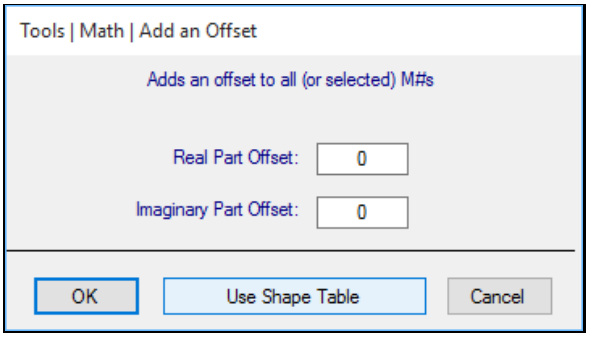
- When executed, the following dialog box opens



- The **Use Shape Table** button scales each **M#** with a ***different scale factor*** from a Shape Table (**SHP**).
- The ***magnitude & phase*** of each **M#** of the ***first shape*** in the Shape Table (**SHP**) is used to scale each ***matching*** **M#** in the Data Block (**BLK**)

Tools | Math | Add an Offset

Adds a complex (real & imaginary) offset to ***all*** (or ***selected***) **M#s**.



- The **Use Shape Table** button adds a ***different offset*** from a Shape Table (**SHP**) to ***each*** **M#**.
- The ***complex*** value for each **M#** of the ***first shape*** in the Shape Table (**SHP**) is used to offset each ***matching*** **M#** in the Data Block (**BLK**).

Tools | Math | Add Random Noise

Adds random noise to each **M#**.

- The amount of random noise is a percentage of the ***maximum magnitude*** of each **M#**.

Tools | Math | Conjugate M#s

Replaces each ***complex*** measurement value with its ***complex conjugate***

- The **Real** part remains the same and the **Imaginary** part is ***multiplied*** by **"-1"**.

Tools | Math | Invert M#s

Replaces each **M#** with its ***inverse***.

Tools | Math | Square M#s

Replaces each **M#** with its ***value squared***.

Tools | Math | Square Root of M#s

Replaces each M# with the ***square root of its value***.

Tools | Math | Smooth M#s

Performs multi-point smoothing of each measurement in a Data Block (**BLK**).

- Replaces each measurement sample with the ***average value*** of **N** samples of data surrounding that sample
  - For example, for **N = 3,**

    M# (sample) = {M# (sample) + M# (sample-1) + M# (sample +1) } / 3

Tools | Math | Re-Sample M#s

Changes the number of samples in a Data Block (**BLK**) without changing the X-Axis span by ***re-sampling the*** **M#s**.

Tools | Math | Sum M#s

Sums ***all*** (or ***selected***) **M#** values at each sample and stores the result into a single **M#**.

Tools | Math | Average M#s

Divides the ***sum*** of ***all*** (or ***selected***) **M#** values at each sample by the number of **M#s** and stores the result into a single **M#**.

Tools | Math | Add (Subtract, Multiply, Divide) a selected M#

Performs the indicated operation between the **M#s** in a Data Block (**BLK**) and a ***selected* M#** in the same or a different Data Block (**BLK**).

- If two Data Block (**BLK**)s have the ***same number*** of **M#s**, you can choose to perform the operation ***between* M# pairs** in the two Data Block (**BLK**)s

Tools | M# Matrix | Add (or Subtract) M# Matrix Data Blocks

Adds a **M# Matrix** Data Block (**BLK**) to the ***host* M# Matrix** Data Block (**BLK**) or **subtracts** a **M# Matrix** Data Block (**BLK**) from the ***host M#* Matrix** Data Block (**BLK**). The ***host*** Data Block (**BLK**) is the one from which this command is executed

- A **M# Matrix** Data Block (**BLK**) is defined by the **Roving & Reference DOFs** of its **M#s**
  - The **Roving DOF** designates the ***row position*** of the **M#** in the **M#** Matrix. The **Reference DOF** designates the ***column position*** of the **M#** in the **M#** Matrix

Tools | M# Matrix | Multiply M# Matrix Data Blocks

Multiplies the ***host* M# Matrix** Data Block (**BLK**) by another **M# Matrix** Data Block (**BLK**). The ***host*** Data Block (**BLK**) is the one from which this command is executed.

- A **M# Matrix** Data Block (**BLK**) is defined by the **Roving & Reference DOFs** of its **M#s**.
- The **Roving DOF** designates the ***row*** position of the **M#** in the **M# Matrix**, The **Reference DOF** designates the ***column*** position of the **M#** in the **M# Matrix**

Tools | M# Matrix | M# Matrix Inverse

Calculates the inverse of the ***host* M# Matrix** Data Block (**BLK**). The ***host*** Data Block (**BLK**) is the one from which this command is executed

- A **M# Matrix** Data Block (**BLK**) is defined by the **Roving & Reference DOFs** of its **M#s**
  - The **Roving DOF** designates the ***row*** position of the **M#** in the **M# Matrix**. The **Reference DOF** designates the ***column*** position of the **M#** in the **M# Matrix**

Tools | Data Block Correlation

Calculates two measures (**MAC** & **SDI**) for comparing **M#s** in two different Data Blocks. **MAC** & **SDI** are calculated between the **M#** values at each sample in one Data Block (**BLK**) with the **M#** values at the same sample in a second Data Block (**BLK**). The results are saved as ***two* M#s** in a new Data Block (**BLK**).

MAC is a measure of the ***co-linearity*** of two shapes. Two shapes are co-linear if they ***"lie on the same Straight line"***.

- **MAC** has values ***between* 0 & 1**
- **MAC = 1** ➔ the M#s in one Data Block (**BLK**) are co-linear with the M#s at the same sample in the other Data Block (**BLK**)
- **MAC *less than* 1** ➔ the M#s in one Data Block (**BLK**) are different from the M#s at the same sample in the other Data Block (**BLK**)

SDI is a measure of the ***difference*** between two shapes.

- **SDI** has values ***between* 0 & 1**
- **SDI = 1** ➔ the **M#s** in one Data Block (**BLK**) are ***the same as*** the **M#s** at the ***same sample*** in the other Data Block (**BLK**)
- **SDI *less than* 1** ➔ the **M#s** in one Data Block (**BLK**) are ***different from*** the **M#s** at the ***same sample*** in the other Data Block (**BLK**)

Tools | M# Pairs Correlation

Calculates two measures (**MAC** & **SDI**) between **M#s *with matching DOFs*** in two Data Blocks. The results are saved as ***two shapes*** in a Shape Table (**SHP**). **MAC** is a measure of the ***co-linearity*** of two **M#s.** Two M#s are co-linear if their values ***"lie on the same Straight line"***

- **MAC** has values ***between* 0 & 1**
- **MAC = 1 ➔** the values of an **M#** in one Data Block (**BLK**) are ***co-linear*** with the values of the **M# *with matching DOF*** in another Data Block (**BLK**)
- **MAC *less than* 1 ➔** the values of an **M#** in one Data Block (**BLK**) are ***different from*** the values of the **M# *with matching DOF*** in another Data Block (**BLK**)

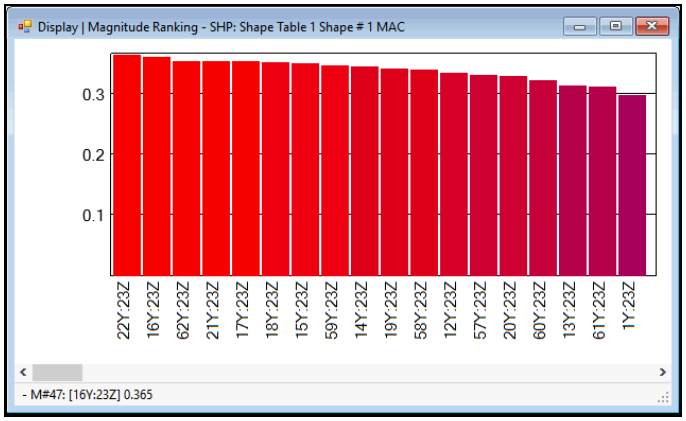
SDI is a measure of the ***difference*** between two **M#s**.

- **SDI** has values between **0 & 1**
- **SDI = 1 ➔** values of an **M#** in one Data Block (**BLK**) are ***the same as*** the values of the **M# *with matching DOF*** in another Data Block (**BLK**)
- **SDI *less than* 1 ➔** values of an **M#** in one Data Block (**BLK**) are ***different from*** the values of the **M# *with matching DOF*** in another Data Block (**BLK**)

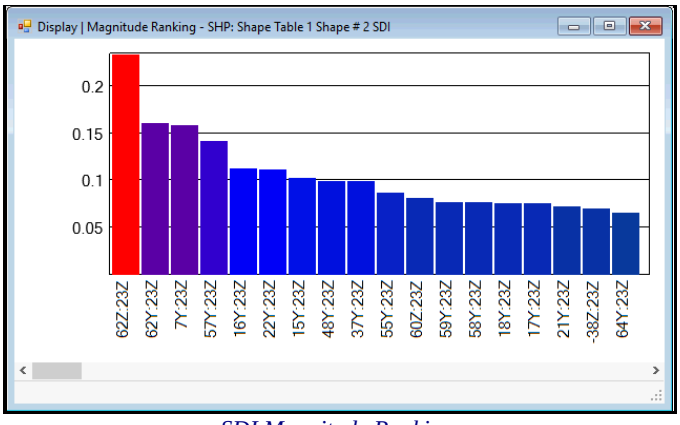
Displaying MAC & SDI Magnitude Ranking Bars

A good way to examine the MAC & SDI values that were saved in a Shape Table (**SHP**) is to use the **Display | Magnitude Ranking** command in the Shape Table (**SHP**).

- Execute **Display | Magnitude Ranking**
  - ***Select* Shape #1** to display **MAC magnitudes** as shown below
  - ***Select* Shape #2** to display **SDI magnitudes** as shown below



MAC Magnitude Ranking.



SDI Magnitude Ranking.

Tools | Tachometer Peak Finder

Returns the X-Axis value of a peak when the Y-Axis value exceeds a threshold level in the ***first (or selected)*** **M#**.

Parameters

- X-Axis
  - Percentage (1 to 100 of the **Block Size)**
  - Sample (1 to the **Block Size**)
  - X-Axis Units (Hz, RPM, CPM, Sec, milli-sec, micro-sec)
- Start of X-axis search range
- End of X-axis search range
- Minimum peak value (in Y-axis units)
- Threshold (percentage of peak value in the search range)
- Script variable name

Tools | Log Decrement

Calculates the ***damping decay constant*** for each **TWF** using the **Logarithmic Decrement** method.

- The **Logarithmic Decrement** method is used to calculate the ***damping decay constant***
- A ***straight line*** is curve fit to the Log Magnitude of each **TWF**, and its slope is ***damping decay constant***
  - The ***damping decay constant*** is the coefficient of the exponential decay envelope on a ***decaying sinusoidal response***
  - For a single resonance, the ***damping decay constant*** is the same as the ***modal damping in Hz*** obtained from curve fitting the **TWF**

Tools | Save Cursor at Samples

Saves the cursor values (Line, Peak, or Band cursor) for ***all*** (or ***selected***) **M#s** of a **frequency domain Data Block** into a new Data Block and applies the **Inverse FFT** to the data.

- This command provides ***band-limited TWFs*** in the new Data Block

Tools | M# Envelope

Peak-hold averages all (or selected) M#s in a Data Block (**BLK**), displays the Envelope and adds it to the end of the M#s spreadsheet.

- **Peal-hold averaging** saves the **peak magnitude** value at each sample of all (or selected) **M#**s

Data Block (BLK) Transform Menu

Transform | Block Size

Changes the Block Size of a Data Block **(BLK)** file. When executed, the **File | Data Block** (**BLK**) **Properties** dialog box is opened, where the Block Size can be edited.

- **Block Size** is the ***number of samples*** (time or frequency) in all the **M#s** of a Data Block (**BLK**)
- ***All* M#s** in a Data Block (**BLK**) must have the ***same* Block Size** in order to support **ODS** display and animation from a Data Block (**BLK**)

Increasing the Block Size

When the Block Size is ***increased***, more samples (with ***zero Y-axis*** values) are added to the end (**right side**) of each **M#.**

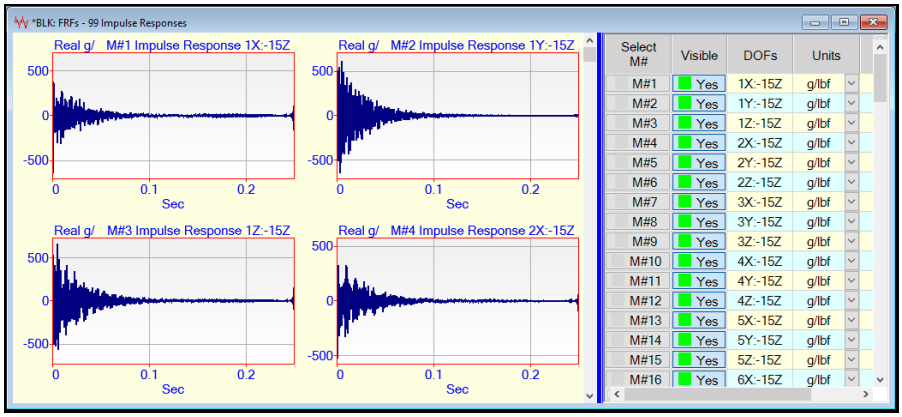
Decreasing the Block Size

When the Block Size is ***decreased***, samples are deleted from the end (**right side**) of each **M#.**

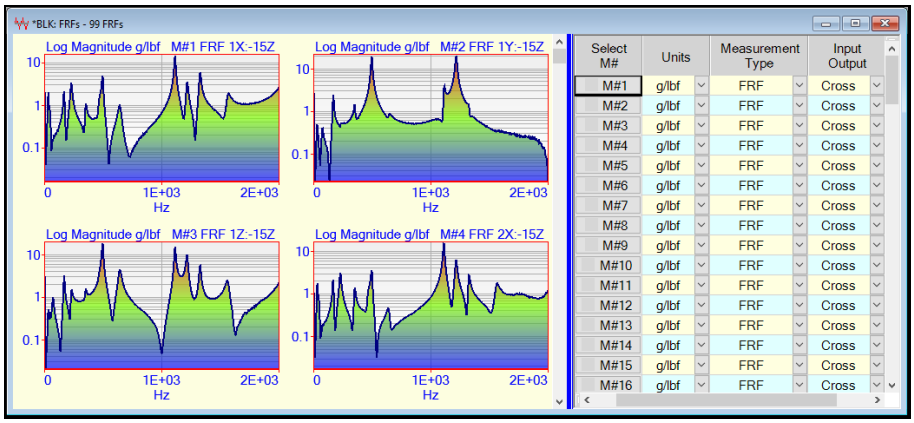
Transform | FFT

Applies the Fast Fourier Transform **(FFT)** algorithm to transform ***each* time domain M#** in a Data Block (**BLK**) into its **frequency spectrum (DFT)**.

- The FFT is a ***loss-less*** (also called ***one-to-one & onto***) transformation from one domain (time or frequency) to the other
- An original **TWF** can ***always be recovered*** by applying the ***Inverse FFT*** to its DFT



*Data Block (**BLK**) Before FFT.*



*Data Block (**BLK**) After FFT.*

Prime Number FFT

MEscope uses a ***prime number* FFT**, which ***does not require*** that the **Block Size** (number of samples) be ***equal to a power of 2***.

One-Sided Versus Two-Sided FFT

All the energy in a time domain signal is spread of ***all*** frequencies, including both ***positive*** & ***negative*** frequencies in its DFT.

- The FFT always calculates a **Two-Sided FFT**, where ***half*** of a signal is represented by ***positive*** frequencies, and ***half*** by ***negative*** frequencies in its spectrum
- A **One-Sided FFT** yields spectrum values ***that are twice*** the values of a **Two-Sided FFT**
- The frequency spectrum of a ***real*** valued **TWF** is ***symmetric*** about zero frequency **(DC)**, so only the ***positive frequency*** half of the spectrum is displayed
- The ***amplitude & power*** values of a **DFT** calculated with a **Two-Sided FFT *are half*** of the values of the its corresponding **TWF**
- The ***amplitude*** & ***power*** values of a **DFT** calculated with a **One-Sided** FFT ***are the same*** values as its corresponding **TWF**

Transform | Inverse FFT

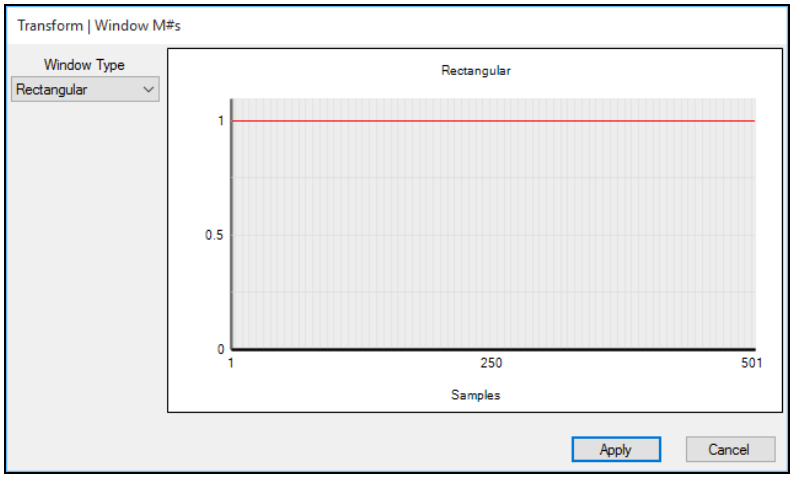
Applies the **Inverse Fast Fourier Transform (IFFT)** to ***each* frequency domain M#** in a Data Block (**BLK**) yielding its corresponding **TWF**.

- The FFT is a ***loss-less*** (also called ***one-to-one & onto***) transformation from one domain (time or frequency) to the other
- An original **TWF** can ***always be recovered*** by applying the **Inverse FFT** to its **DFT**

Transform | Window M#s

Multiplies ***all*** (or ***selected***) **M#s** by one of several windowing functions.

- When executed, the following window is opened,

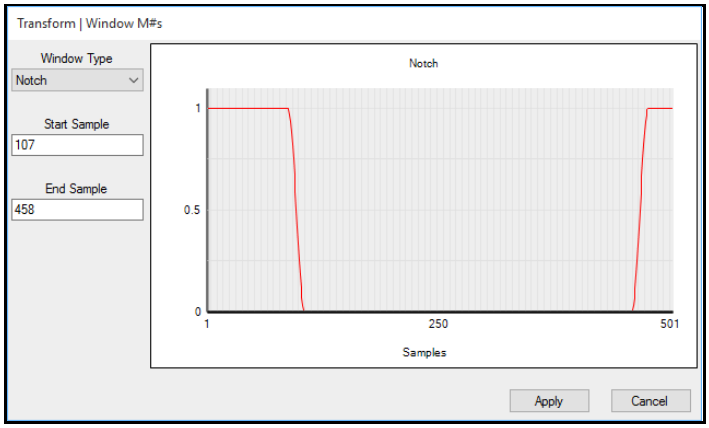


*Window **M#s** Dialog Box Showing the Rectangular Window.*

Notch Window

The **Notch** window is useful for ***removing (zeroing) unwanted*** samples of data. It uses a **Cosine function** to transition the data ***smoothly to zero inside*** the cursor band. The **Notch** window is defined as follows,

- Outside the cursor band, **Notch ➔ 1.0**
- From **0% to 5% inside** the cursor band, **Notch ➔ Cos(0) =1.0** to **Cos(90) = 0.0**
- From **5% to 95% inside** the cursor band **Notch ➔ 0.0**
- From **95% to 100% inside** the cursor band **Notch ➔ Cos(90) = 0.0** to **Cos(0) = 1.0**



Notch Window.

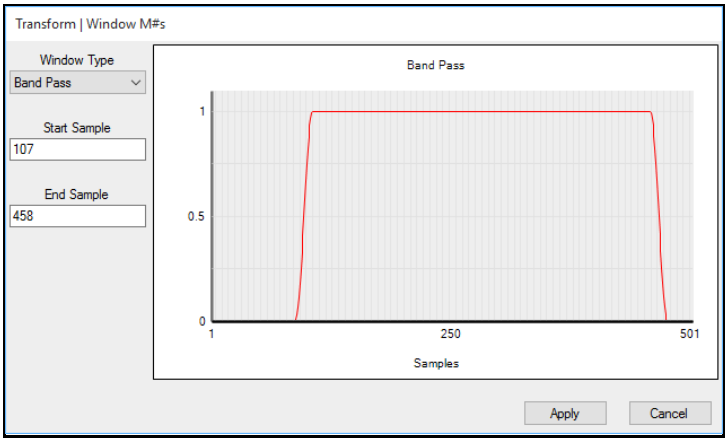
To apply a Notch window,

- ***Select*** the **M#s** to be windowed
- Display the **Band** cursor and position the band to enclose the data to be notched (or zeroed)
- Execute **Transform | Window M#s**, select the Notch window, and ***press*** **Apply**

Band Pass Window

The **Band Pass** window is useful for preserving certain samples of data and setting the rest to zero. It uses a Cosine function to transition the data ***smoothly to zero outside the cursor band***. The **Band Pass** window is defined as follows,

- **Inside** the cursor band, **Band Pass ➔ 1.0**
- For **5% of the cursor band prior to the lower edge, Band Pass ➔ Cos (90) = 0.0** to **Cos (0) = 1.0**
- For **5% of the cursor band following the upper edge**, **Band Pass ➔ Cos (0) = 1.0** to **Cos (90) = 0.0**
- **Otherwise**, **Band Pass ➔ 0.0**



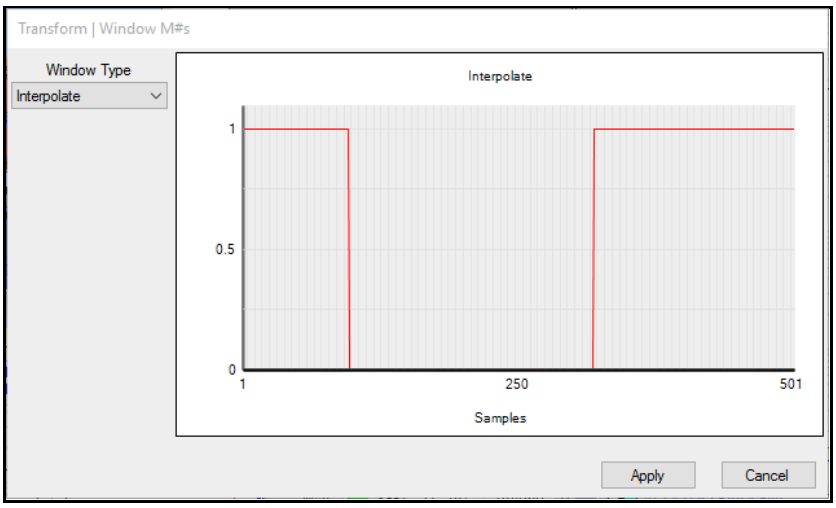
Band Pass Window.

To apply the Band Pass window,

- ***Select*** the **M#s** to be windowed
- Display the **Band** cursor, and position the band to enclose the data to be preserved
- Execute **Transform | Window M#s**, select the Band Pass window, and ***press*** **Apply**

Interpolation Window

This window is used for replacing ***unwanted data*** with ***interpolated data*** in a band of samples. Data in the cursor Band is replaced with a ***Straight Line of data*** between the values at the ends of the band

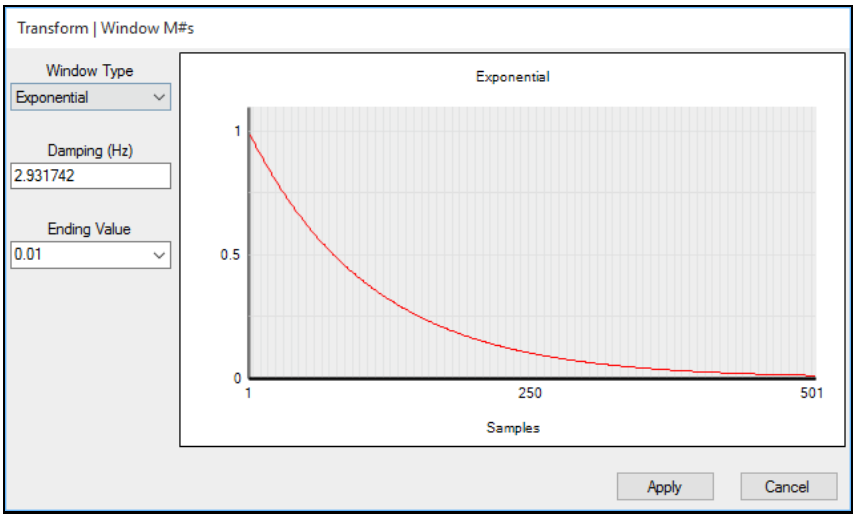


Interpolation Window.

Exponential Window

This window multiplies ***each*** **TWF M#** by a ***decreasing*** (or ***increasing***) exponential curve.

- The **beginning value** of the exponential window is **"1"**
- **Ending value *greater than "0"*** & ***less than "1"*** ➔ decreasing exponential window is applied
- **Ending value *greater than "1"*** ➔ increasing exponential window is applied



Exponential Window.

Exponential Windowing of Frequency Domain M#s

When the exponential window is applied to **frequency domain M#s**, the following steps are carried out

- ***All*** (or ***selected***) **M#s** are transformed to the time domain using the Inverse FFT
- The **Exponential** window is applied
- The **M#s** are transformed back to the frequency domain using the FFT

Decreasing Exponential Reduces Noise & Leakage

A ***deceasing*** exponential ***modifies each TWF*** in several ways.

- ***Noise is suppressed*** in each **TWF**
- A windowed waveform is ***more completely contained*** within its sampling window, so its spectrum ***has less leakage***
- The damping of all modes is ***artificially increased*** by a known amount of damping
- All ***resonance peaks become wider***, meaning that tightly-coupled modes are less widely-separated

Increasing Exponential Narrows Resonance Peaks

An **in*creasing*** exponential modifies **each TWF** in several ways.

- ***Noise is amplified*** in each **TWF**
- The waveform is ***less completely contained*** within its sampling window, so its **Digital Fourier Transform *has more leakage***
- The damping of all modes is ***artificially decreased*** by a known amount of damping
- All ***resonance peaks become narrower***, meaning that tightly-coupled modes are more widely-separated

Modal Damping

Applying an exponential window to **M#s** that contain resonant vibration ***adds or subtracts a known amount of damping*** to each of the modes represented in the data.

Following curve fitting, the exponential window damping is ***added to or subtracted from the damping*** of each mode shape when it is are saved into a Shape Table (**SHP**)

- A ***decreasing*** **exponential** window ***adds damping*** to each mode, which is ***subtracted*** from their modal damping when mode shapes are saved into a Shape Table (**SHP**)
- An ***increasing*** **exponential** window ***subtracts damping*** from each mode, which is ***added*** to their modal damping when mode shapes are saved into a Shape Table (**SHP**)

The amount of modal damping added by the Exponential window ***is cumulative***

- If the Exponential window is ***applied several times*** to the same data, the amount of damping is the ***sum of the damping amounts*** added with each application of the window

The ***damping*** added by an Exponential window to the modes is listed in the **Transform | Window M#s** dialog box, and in the **Window Value** column of the **M#s** spreadsheet

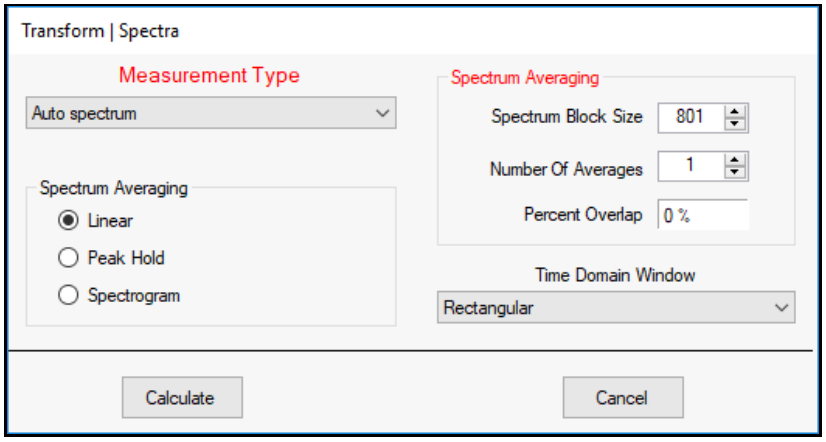
Modal Damping Change Following Curve Fitting

The damping of each mode is either ***decreased or increased*** when one of the following commands is executed,

- **Save Shapes** button on the **Residues Save Shapes** tab
- **Curve Fit | Shapes | Save Shapes**

Transform | Spectra

Calculates **Fourier spectra**, **Auto & Cross spectra, PSDs** or **ESDs** from **TWF**s or frequency spectra. When this command is executed, the dialog box below is opened



Digital Fourier Transform (DFT)

A **Digital Fourier Transform** is also called the **DFT** of a **TWF**.

- The FFT calculates the **Digital Fourier Transform (DFT)** of each **M#** in a Data Block (**BLK**)

Auto spectrum (APS)

Each Auto spectrum is calculated by multiplying the **DFT** of a **TWF** by the ***complex conjugate*** of its **DFT**.

- The Auto spectrum is **Real valued** (magnitude only)

Cross spectrum (XPS)

Each Cross-spectrum is calculated by multiplying the **DFT** of a **TWF** labeled as an **Output** by the ***complex conjugate*** of the **DFT** of a **TWF** labeled as an **Input**.

- Each Input & Output is designated in the **Input Output** column of the **M#s** spreadsheet in a Data Block (**BLK**) window.
- The Cross spectrum is complex valued with **magnitude & phase**

Power Spectral Density (PSD)

A **PSD** is an Auto spectrum that has been ***"normalized"*** by dividing it by the frequency resolution of the Auto spectrum.

- If the units of an Auto spectrum are **g^2**, the units of its corresponding **PSD** are **g^2 / Hz**

Energy Spectral Density (ESD)

An **ESD** is a **PSD** ***multiplied by the time length*** **(T)** of the **TWF** used to create the **PSD**. An **ESD** is used to characterize **transient signals**.

- Units of a **PSD ➔ g^2 / Hz**
- Units of its **ESD ➔ (g^2 - sec) / Hz**

Spectrogram

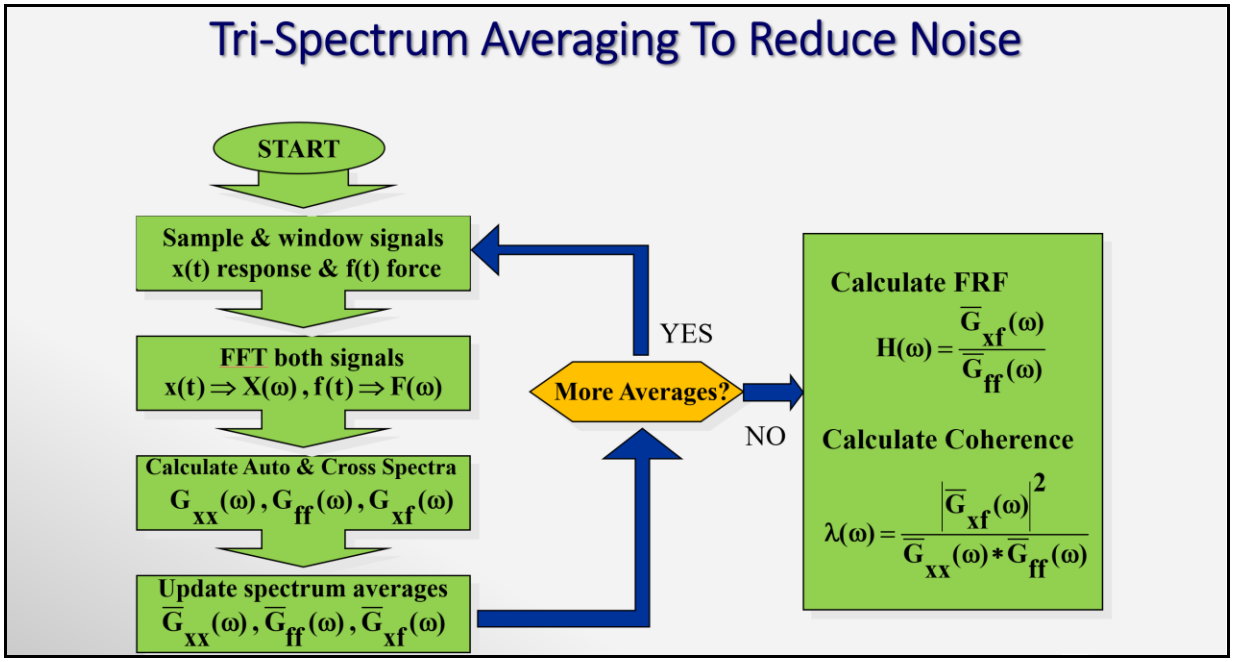
A Spectrogram is a series of spectra that are calculated from ***short time portions*** of a **TWF**.

- If **Number of Spectrum Averages = 10 ➔** the Spectrogram contains 10 individual spectrum estimates

Spectrum Averaging

Spectrum averaging is done to remove extraneous noise from vibration signals. Spectrum averaging can be used to calculate Auto & Cross spectra as well as **ODS-FRFs** and **FRFs**, (which are both calculated from Auto & Cross spectra). A spectrum averaging loop is depicted in the diagram below

- An **average Auto spectrum** is calculated by averaging together multiple Auto spectrum estimates
- An **average Cross spectrum** is calculated by averaging together multiple Cross spectrum estimates
- **ODS-FRFs** & **FRFs** are calculated from **averaged Auto & Cross spectra**.



Block Diagram of a Spectrum Averaging Loop.

Total Samples Required

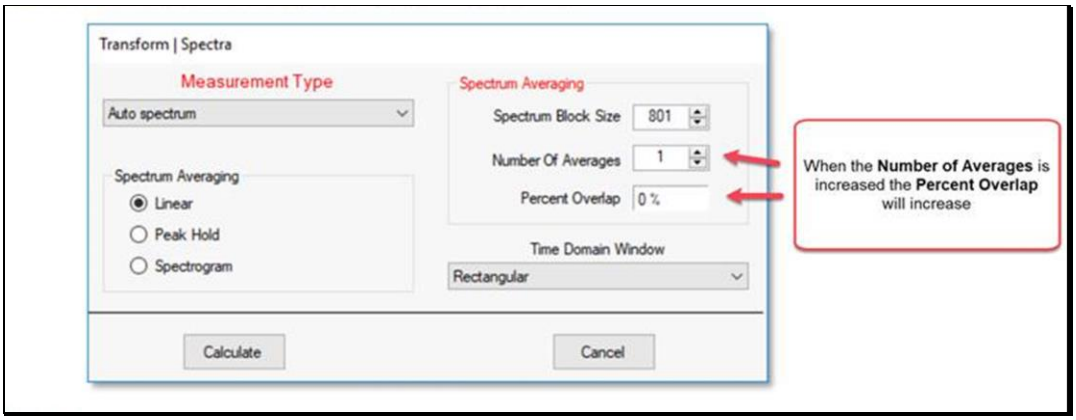
The total number of samples required for spectrum averaging is,

Total Samples Required = [2 x Spectrum Block Size x Number of Averages]

Overlap Processing

If the **Total Samples Required** ***exceeds the time domain Block Size***, Overlap Processing will be used during spectrum averaging

- During Overlap Processing, each sampling window of **TWF**s used to calculate a spectrum estimate overlaps with the sampling window used to calculate the previous spectrum estimate



Transform | Seed TRN Chain

Seeds a **Transmissibility (TRN) chain** with a single measurement (Auto spectrum, Cross spectrum, **FRF**) to yield a set of ***single reference* ODS-FRFs, Cross spectra, or FRFs**.

- A **Transmissibility** is defined as the **DFT** of a vibration response divided by the **DFT** of another vibration response (acceleration, velocity, or displacement)

A **TRN Chain** is a series of Transmissibility's chained together by their DOFs, the **Roving DOF** of one Transmissibility matching the **Reference DOF** on another

- For example, the following is a **TRN Chain**; **TRN** (**1Z:2Z**), **TRN** (**2Z**:**3Z**), **TRN** (**3Z**:**4Z**), **TRN** (**4Z:5Z**),...

A **TRN Chain** has several advantages,

- Only Structural responses are required to form a **TRN Chain**
- Data can be acquired with ***two sensors attached close to each other*** throughout the test
- ***Either or both* sensors** can be moved between acquisitions
- A **TRN Chain** can be formed from data acquired from an ***operating machine*** or from any structure where the ***excitation forces are not measured***
- A **TRN Chain** accounts for changes in excitation force levels during data acquisition
- Before executing this command, the **M#** used to seed a **TRN Chain *must be stored in the same* Data Block (BLK)** as the **TRN Chain**

Seeding a TRN Chain

Seeding a **TRN** Chain will give several different single reference functions

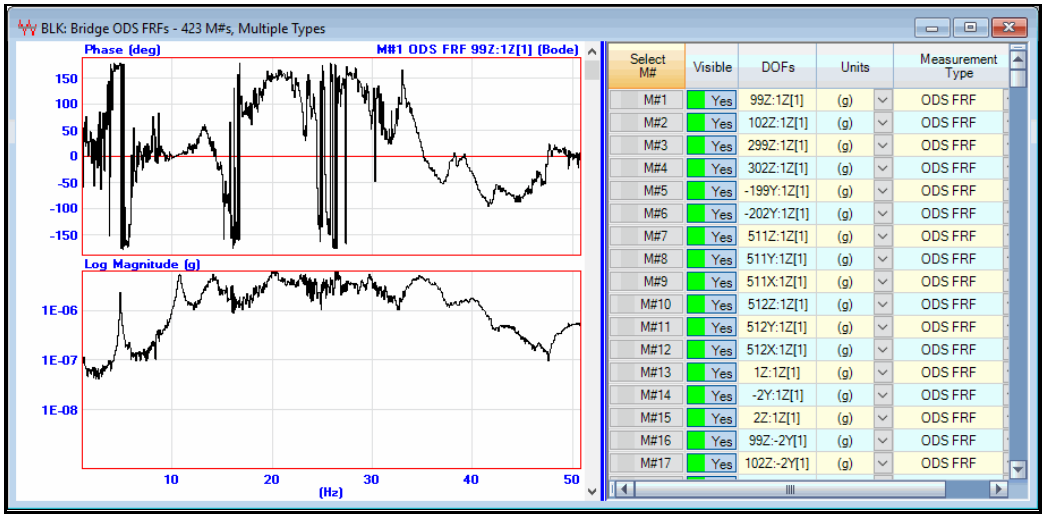
- Seeding (multiplying) a **TRN** Chain by an Auto spectrum ➔ a set **of *single reference* ODS-FRFs**
- Seeding (multiplying) a **TRN** Chain by a Cross spectrum ➔ a set of ***single reference* Cross spectra**
- Seeding (multiplying) a **TRN** Chain by an **FRF** ➔ a set of ***single reference* FRFs**

Transform | ODS-FRFs

Calculates a set of **ODS-FRFs** from operational (or **output-only**) data.

What is an ODS-FRF?

An **ODS-FRF** has a magnitude equal to the Auto spectrum of a Roving response and the phase between the Roving response and a **(fixed) Reference** response. An **ODS-FRF** is a ***complex valued frequency domain function*** that is like an **FRF**.



*Typical **ODS-FRF**.*

Advantages of ODS-FRFs

The **ODS-FRF** provides the true response (in displacement, velocity, or acceleration units) at each DOF of a machine or structure, together with its phase relative to a Reference response.

- An **ODS-FRF** ***contains a peak at each resonant frequency***
- **ODS's** can be displayed in animation from set of **ODS-FRFs**
- **OMA mode shapes** can be extracted by ***curve fitting*** a set of **ODS-FRFs**

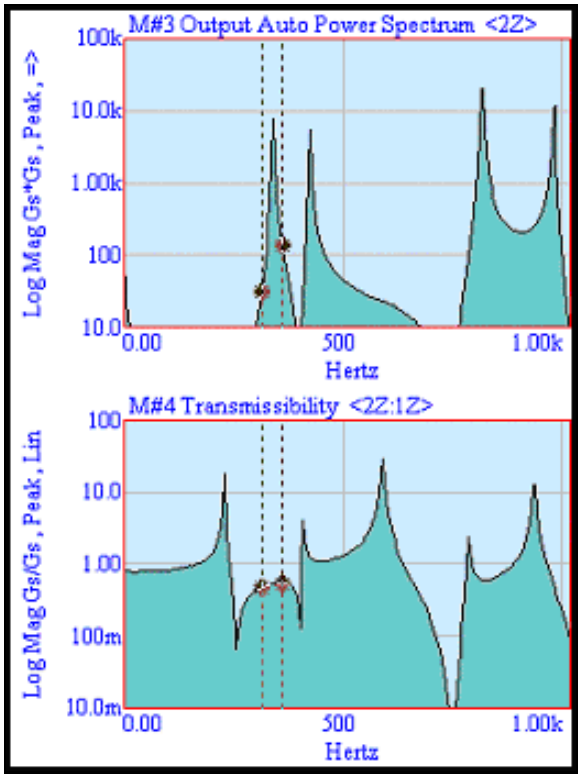
ODS's From a Set of ODS-FRFs

If shape data from the cursor position in two or more **ODS-FRFs** is displayed in animation on a model of the test article, the resulting **ODS** ***is the true overall response*** of the structure at each DOF, with the ***correct phase*** relative to all other DOFs.

What is Transmissibility?

Transmissibility is the **DFT** of a Roving response divided by the **DFT** of a Reference response. Transmissibility is calculated in the same way as an **FRF**, but a ***(fixed) Reference*** response is used instead of the unmeasured excitation force(s)

- **Advantage of Transmissibility:** If the excitation force varies between Measurement Sets, the transmissibility ***is not affected***
  - For a linear dynamic system, any change in both the Roving & Reference responses is ***"canceled out"*** in a Transmissibility
- **Difficulty with Transmissibility:** A Transmissibility has a ”***flat spot” instead of a peak*** in the vicinity of each resonant frequency, as shown below



Roving Auto Spectrum & Transmissibility.

Transmissibility's Multiplied by Reference Auto Spectrum

When a set of Transmissibility's is multiplied by a ***single Reference Auto spectrum***, the result is a set of **ODS-FRFs**.

(Transmissibility's x Reference Auto Spectrum) ➔ ODS-FRFs

Operating Mode Shapes from ODS-FRFs

At or near a resonant frequency, the **ODS** obtained from a set of **ODS-FRFs *is often dominated*** by the mode shape of that resonance.

- A windowed set of **ODS-FRFs** can be curve fit using a **FRF-based curve fitting method** to obtain an **OMA mode shape** for each resonance

Data for Calculating ODS-FRFs

Before executing this command, all the data necessary for calculating **ODS-FRFs** much be **contained in one Data Block.**

The **Transform | ODS-FRFs** command can calculate **ODS-FRFs** from ***three different kinds of data***.

1. **TWFs ➔** Multiple Roving responses and a Reference response.
2. **Auto & Cross Spectra ➔** Roving response Auto spectra and Cross spectra between each Roving response and a Reference response.
3. **TRNs & Reference Auto Spectrum ➔** Transmissibility's between each Roving response and a Reference response and the Reference Auto spectrum.

TWFs ➔ ODS-FRFs

Each **TWF M#** must contain the **DOF** (point & direction) from which it was acquired including its [**measurement set**]

- Roving responses must be defined as **Outputs** in the **Input Output** column of the **M#s** spreadsheet
- Reference responses must be defined as **Inputs** in the **Input Output** column of the **M#s** spreadsheet

Auto & Cross spectra ➔ ODS-FRFs

Each Auto spectrum **DOF** must match the **Roving DOF** of a Cross spectrum

- Auto spectra must be defined as **Outputs** in the **Input Output** column of the **M#s** spreadsheet
- Cross spectra must be defined as **Cross** in the **Input Output** column of the **M#s** spreadsheet

Transmissibility's ➔ ODS-FRFs

- Transmissibility's must be defined as **Cross** in the **Input Output** column of the **M#s** spreadsheet
- The Reference Auto spectrum must be defined as an **Input** in the **Input Output** column of the **M#s** spreadsheet

Multiple Measurement Sets

If the **M# DOFs** contain [**Measurement Set]** numbers, each Measurement Set is processed independently of the other Measurement Sets.

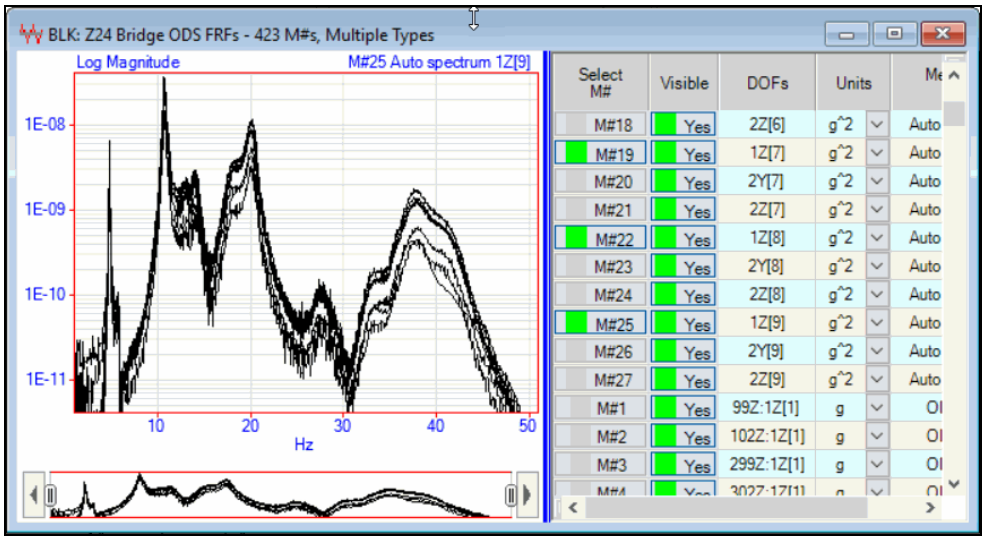
Transform | Scale ODS-FRFs

Re-scales* ODS-FRFs** to correct for changes in the response levels between ***multiple Measurement Sets.

- This command is only required when **ODS-FRFs** are calculated from ***multiple Measurement Sets*** of data

Overlaid Reference Auto Spectra

If the Reference Auto Spectra ***from all Measurement Sets*** are overlaid as shown below, changes of response levels between Measurement Sets will be apparent.



*Overlaid **Reference Auto Spectra** from Multiple Measurement Sets.*

ODS-FRF Scale Factor

To re-scale the **ODS-FRFs**, all **ODS-FRFs** in **Measurement Set [i]** are multiplied by the **Scale Factor (i)**

$$\text{ScaleFactor}(i) = \frac{1}{N}\left(\frac{\sum_{i=1}^{N}\text{ARM}(i)}{\text{ARM}(i)}\right)$$

N = Number of Measurement Sets

ARM(i) = **Average Magnitude** of the **Reference Auto spectrum** for **Measurement Set [i]**

- If the **Line** cursor is displayed, **ARM(i)** is calculated at the **Line** cursor position
- If the **Band** or **Peak** cursor is displayed, **ARM(i)** is calculated using all the samples in the band
- If no cursors are displayed, **ARM(i)** is calculated using ***all samples*** of each Reference Auto spectrum

What is a Multi-Input Multi-Output (MIMO) Model?

A **MIMO** model is a frequency domain model where the **DFTs** of ***multiple*** Inputs are multiplied by elements of an **FRF *matrix*** to yield the **DFTs** of ***multiple*** Outputs. A **Multi-Input Multi-Output (MIMO)** dynamic model is used to calculate multiple **Inputs**, **Outputs & FRFs** of a structure.

- The **MIMO** Model is written as,

  {X(ω)} = [H(ω)] {F(ω)}

  {F(ω)} ➔ Input **DFT** (**m - vector**)

  [H(ω)] ➔ **FRF** matrix (**n by m**)

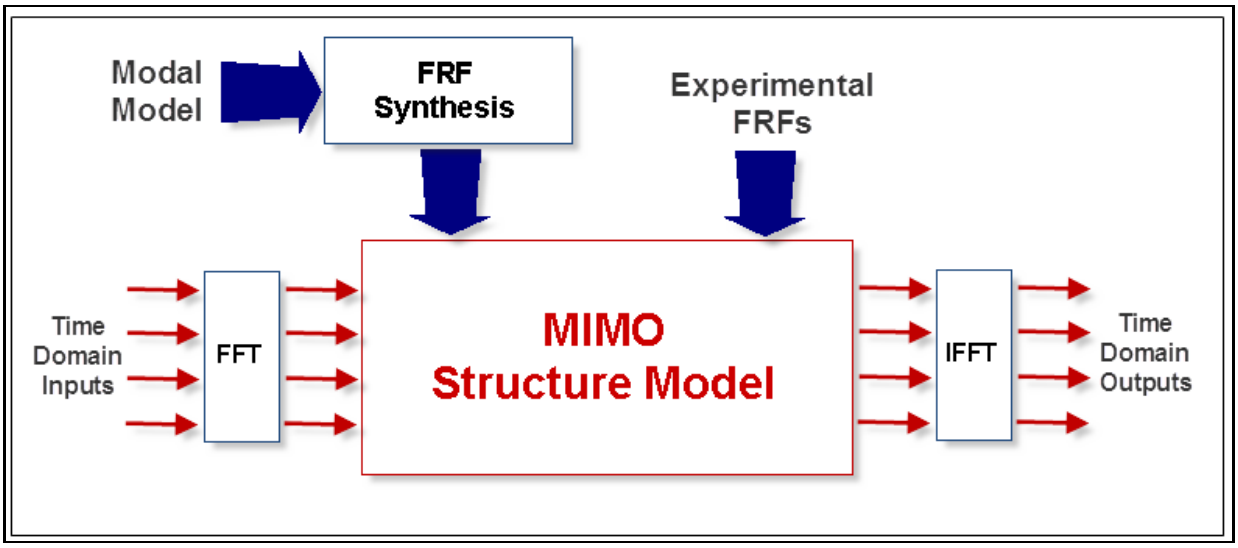
  {X(ω)} ➔ Output **DFT** (**n - vector**)

  m ➔ number of Inputs

  n ➔ number of Outputs

  ω ➔ frequency variable (radians per second)

- ***Rows*** of the **FRF** matrix correspond to **Outputs** and ***columns*** correspond to **Inputs**
- **Each Input** and **each Output** has a DOF (point & direction)
- **Each FRF** is a ***cross-channel measurement*** between an Input DOF and an Output DOF



***MIMO** Model Block Diagram*

Each part of a **MIMO** model (**Inputs**, **Outputs**, **FRFs**) ***is calculated from the other two parts***.

- Inputs & Outputs can be either **TWFs** or **frequency domain functions**
- Frequency domain functions can be **DFTs, Auto & Cross spectra, or PSDs**
- **FRFs** can be either **measured or synthesized** from a **modal model**

Frequency Response Function (FRF)

An **FRF** is defined as the **DFT** of a ***displacement, velocity, or acceleration*** response ***divided by*** the **DFT** of the ***excitation force*** that caused the response.

Transmissibility (TRN)

A **Transmissibility** is defined as the **DFT** of an Output divided by the **DFT** of a Reference Output

M# Input Output Properties

Before using one of the **Transform** commands, ***each*** **M#** must be designated as either an **Input**, **Output**, **Both** or **Cross** in the **Input Output** column of the **M#s** spreadsheet.

- **Input M#s** must be designated as **Input** or **Both** in the **Input Output** column of the **M#s** spreadsheet
- **Output M#s** must be designated as **Output** or **Both** in the **Input Output** column of the **M#s** spreadsheet
- **Transfer Function M#s** must be designated as **Cross** in the **Input Output** column of the **M#s** spreadsheet

M# DOFs and Units

Before using one of the **Transform** commands, each M# must have correct DOFs and engineering units.

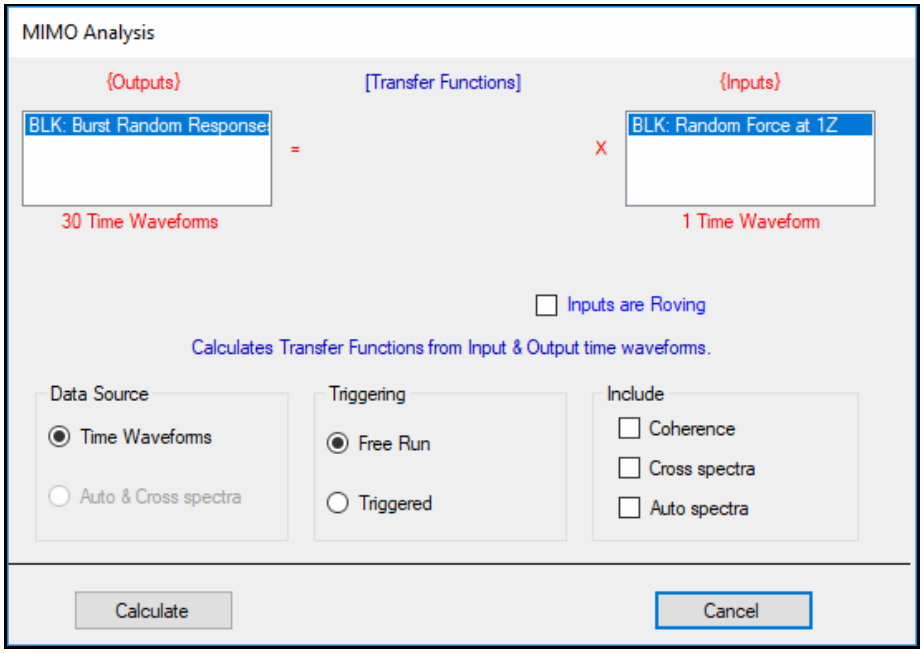
- ***Each*** **M#** must have a **DOF** in the **DOFs** column of the **M#s** spreadsheet that designates the Point & direction of its measurement
- ***Each*** **M#** must have ***correct engineering units*** in the **Units** column of the **M#s** spreadsheet

Transform | H1 FRF

Calculates **H1 FRFs** from **TWF**s or frequency spectra in a Data Block (**BLK**).

- H1 **FRFs** can be calculated from two sources
  - **Input** & **Output TWF**s
  - **Input Auto spectra** and **Cross spectra** between Inputs & Outputs

When this command is executed, the following dialog box will open.



H1 FRFs Using Auto & Cross Spectra

An H1 **FRF** matrix is calculated from **Auto & Cross spectra** using the following formula,

$[H1\ FRF(\omega)] = [\{X(\omega)\}\ \{F(\omega)\}^t]\ [\{F(\omega)\}\ \{F(\omega)\}^t]^{-1}$

[H1 FRF(ω)] ➔ **H1 FRF** matrix (**n by m**)

[{X(ω)} {F(ω)}ᵗ] ➔ Cross spectrum matrix between Outputs & Inputs (**n by m**)

[{F(ω)} {F(ω)}ᵗ] ➔ Input Auto spectrum matrix (**m by m**)

{F(ω)} ➔ **DFTs** of Inputs (**m-vector**)

{X(ω)} ➔ **DFTs** of Outputs (**n-vector**)

m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔ denotes conjugate transposed

-1 ➔ denotes the matrix inverse

H1 FRFs Using TWFs

If **TWFs** are used to calculate **FRFs**, ***time domain windowing, overlap processing***, and ***spectrum averaging*** can be used to calculate Auto & Cross spectra, which are then used to calculate the **FRFs** using the formula above.

- **Coherences, Auto spectra & Cross spectra** can also be calculated and saved with the **FRFs** by ***checking*** them in the **Include** section of the dialog box

Time Domain Windowing

Sampled **TWF**s can have different windows applied to them before the FFT is applied. Each window is most effective when used on a specific type of data, as described below.

- **Rectangular** (for signals that are ***periodic in the time domain sampling window***)
- **Hanning** (for ***broad band*** signals that are ***not completely contained in the time domain sampling window***)
- **Flat Top** (for ***narrow band*** signals)

Transform | H2 FRFs

Calculates **H2 FRFs** from **TWF**s or frequency spectra in a Data Block (**BLK**).

- H2 **FRFs** can be calculated from
  - **Input** & **Output TWF**s
  - **Output Auto spectra** and **Cross spectra** between Inputs & Outputs

An **H2 FRF** matrix is calculated using the following formula.

[H2 FRF(ω)] = [X(ω)^t X(ω)] / [X(ω)^t F(ω)]

[H2 FRF(ω)] ➔ H2 **FRF** matrix (**n by m**)

[X(ω)^t F(ω)] ➔ Cross spectrum between Output & Input (**n by m**)

[X(ω)^t X(ω)] ➔ Output Auto spectrum (**n by n**)

{F(ω)} ➔ **DFTs** of Inputs (**m-vector**)

{X(ω)} ➔ **DFTs** of Outputs (**n-vector**)

ω ➔ frequency variable (radians per second)

t ➔ denotes complex conjugate

Transform | Outputs

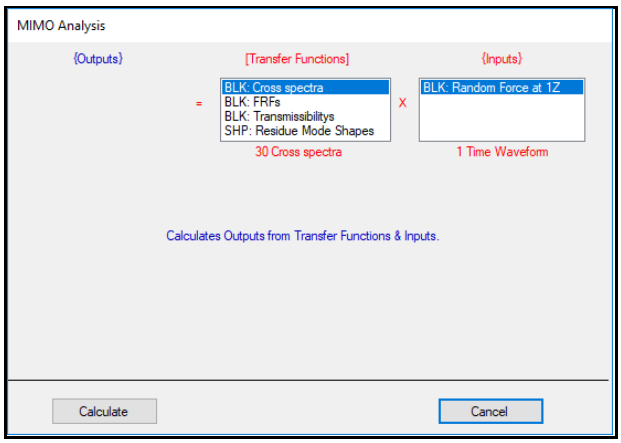
Calculates ***multiple*** **Outputs** from **FRFs** & **Inputs**. Different types of **Inputs** can be used for this calculation,

- Input **TWF**s
- Input Auto spectra or Fourier spectra

Before using this command,

- Inputs must be designated as **Input** (or **Both**) in the **Input Output** column of the **M#s** spreadsheet
- **FRFs** must be designated as **Cross** in the **Input Output** column of the **M#s** spreadsheet
- Residue mode shapes or UMM mode shapes can also be used to ***synthesize*** the required **FRFs**

When this command is executed, the following dialog box is opened,



- The Data Block (**BLK**) containing the **Inputs** is chosen from the **Inputs** list box
- The Data Block (**BLK**) containing the Transfer Functions (**FRFs**, **Cross** measurements, **Mode Shapes**) is chosen from the **Transfer Functions** list box

Outputs from FRFs & Inputs

Outputs are calculated from **FRFs** & **Inputs** in three different ways

1. Output **TWFs** or **Fourier spectra** are calculated from Input **TWF**s or Fourier spectra & **FRFs**.
2. **Cross spectra** are calculated between Inputs & Outputs
3. Output **Auto spectra** or **PSDs** are calculated from Auto spectra or PSDs & **FRFs**

Output DFTs and TWFs

Output **DFTs** are calculated from **FRFs** and **Input DFTs** using the formula,

{X(ω)} = [H(ω)] {F(ω)}

{F(ω)} ➔ **DFTs** of Inputs (**m - vector**)

[H(ω)] ➔ **FRF** matrix (**n by m**)

{X(ω)} ➔ **DFTs** of Outputs (**n - vector**)

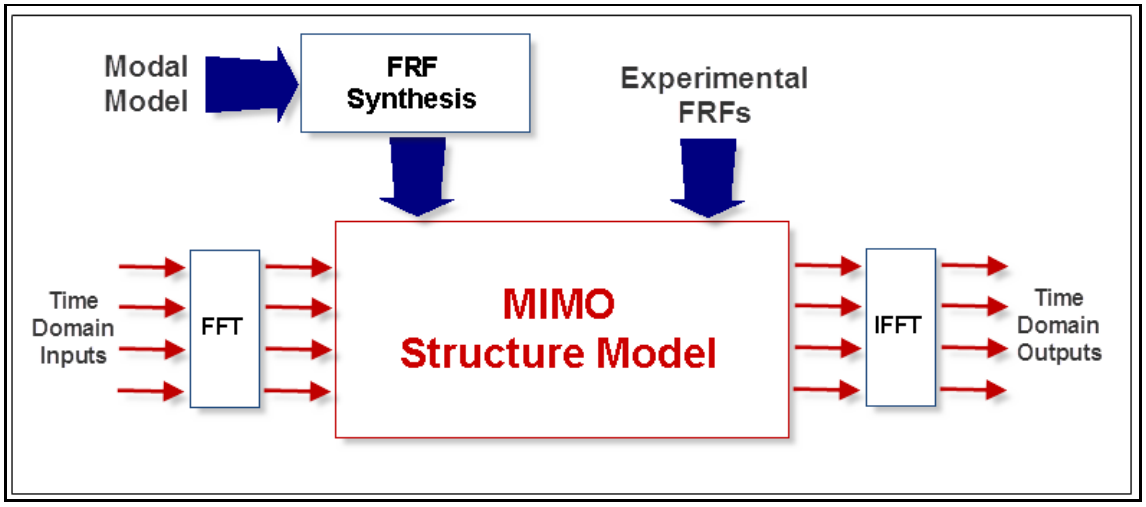
m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

- If **Input TWF**s are provided as a Source, they are transformed to **DFTs** before calculating **Output DFTs**
- The calculated **Output DFTs** are then transformed to **Output TWF**s

The block diagram below depicts Outputs calculation when Inputs are provided as **TWF**s, and either a Modal Model or Experimental **FRFs** are provided as the MIMO matrix.



***MIMO** Output Calculation.*

Cross Spectra

Cross spectra between Inputs & Outputs are calculated from **Input** Auto spectra and **FRFs** using the formula,

$[\{X(\omega)\}\{F(\omega)\}^t] = [H(\omega)][\{F(\omega)\}\{F(\omega)\}^t]$

$[\{X(\omega)\}\{F(\omega)\}^t]$ ➔ Cross spectrum matrix between Inputs & Outputs (**n by m**)

$[\{F(\omega)\}\{F(\omega)\}^t]$ ➔ Input Auto spectrum matrix (**m by m**)

$[H(\omega)]$ ➔ FRF matrix (**n by m**)

m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔ denotes transposed conjugate

Output Auto Spectra

Output Auto spectra or PSDs are calculated from **Input** Auto spectra or PSDs and **FRFs** using the formula,

$[\{X(\omega)\}\{X(\omega)\}^t] = [H(\omega)][\{F(\omega)\}\{F(\omega)\}^t][H(\omega]^t$

$[\{X(\omega)\}\{X(\omega)\}^t]$ ➔Output Auto spectrum matrix (**n by n**)

$[\{F(\omega)\}\{F(\omega)\}^t]$ ➔ Input Auto spectrum matrix (**m by m**)

$[H(\omega)]$ ➔FRF matrix (**n by m**)

m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔ denotes transposed conjugate

- ***Only the diagonal elements*** of the **Output** Auto spectrum matrix are calculated

Input TWFs

TWFs can be imported or synthesized using **File | New | Data Block** in the MEscope window.

- **Input TWF**s are transformed to **DFTs** before being multiplied by the **FRFs** to yield **Output DFTs**
  - The Output **DFTs** are then transformed to **TWF**s

FRFs Synthesized from Modal Parameters

FRFs can be ***imported*** or ***acquired*** with an **Acquisition** window, or ***synthesized*** from a modal model.

If a Shape Table (**SHP**) with a modal model in it is chosen instead of an **FRF** Data Block (**BLK**), the required **FRFs** are ***synthesized from modal parameters***.

The frequency axis parameters of the **Input DFTs** are used for the **FRF** synthesis

- If **Residue mode shapes** are used, **FRFs *can only be synthesized with the same* DOFs** as the Residue mode shapes.
- If **UMM mode shapes** are used, **FRFs *are synthesized*** with **Reference DOFs** to match the DOFs of the **Inputs**

FRF DOFs and the MIMO Matrix

Each **FRF** is assembled into an **FRF matrix** based on its **Output & Input DOFs**.

- The **Output DOF** of an **FRF** designates its ***row position*** in the **MIMO matrix**
- The **Input DOF** of an **FRF** designates its ***column position*** in the **MIMO matrix**
- The DOF of each **Input** must match with an **Input DOF** (***column***) of the **MIMO matrix**
- Each calculated **Output** is given the **Output DOF** (***row***) of the **MIMO matrix**

Transform | Inputs

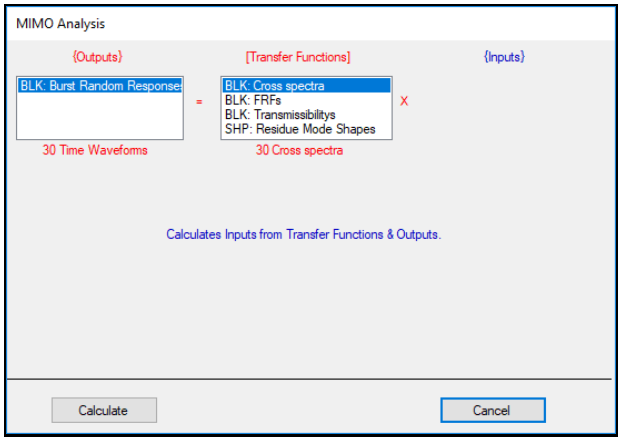
Calculates ***multiple*** **Inputs** from **FRFs** and **Outputs**. Different types of **Output** measurements can be used for this calculation.

- **Output TWF**s
- **Output** Auto spectra, **DFTs**, or **Cross** spectra between Inputs & Outputs

Before using this command

- Outputs must be designated as **Output** (or **Both**) in the **Input Output** column of the **M#s** spreadsheet
- **FRFs** must be designated as **Cross** in the **Input Output** column of the **M#s** spreadsheet
- **Residue mode shapes** or **UMM mode shapes** can also be used ***to synthesize the required*** **FRFs**

When this command is executed, the following dialog box is opened,



Input DFTs or TWFs

Input **DFTs** are calculated from **Output DFTs** and **FRFs** using the formula,

$\{F(\omega)\} = [T(\omega)]\ \{X(\omega)\}$

$[T(\omega)]$ ➔ $[[H(\omega)]^t\ [H(\omega)]]^{-1}\ [H(\omega)]^t$ (m by n) matrix

$[H(\omega)]$ ➔ **FRF** matrix (**n by m**)

$\{F(\omega)\}$ ➔ Input **DFTs** (**m - vector**)

$\{X(\omega)\}$ ➔ Output **DFTs** (**n - vector**)

m ➔ number of Inputs

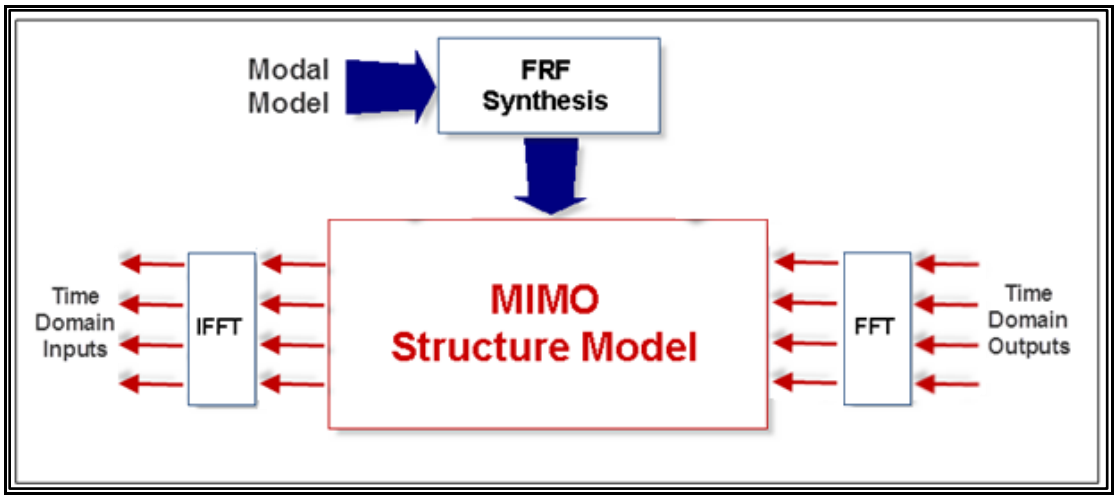
n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔- denotes transposed conjugate

-1 ➔ denotes matrix inverse

- If **Output TWF**s are provided, they are transformed to **DFTs** before solving the above equation.
- The calculated **Input DFTs** are then transformed to **Input TWF**s.



Input Auto spectra From Cross spectra

Input Auto spectra are calculated from **FRFs** and Cross spectra using the formula,

$$[\{F(\omega)\}\{F(\omega)\}^t] = [T(\omega)]\,[X(\omega)\}\{F(\omega)\}^t$$

$[\{F(\omega)\}\{F(\omega)\}^t]$ ➔ Input Auto spectrum matrix (**m by m**)

$[T(\omega)]$ ➔ $[[H(\omega)]^t[H(\omega)]]^{-1}[H(\omega)]^t$ (**m by n**) matrix

$[H(\omega)]$ ➔ **FRF** matrix (**n by m**)

$[\{X(\omega)\}\{F(\omega)\}^t]$ ➔ Cross spectrum matrix (**n by m**)

m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔ denotes transposed conjugate

-1 ➔ denotes matrix inverse

Input Auto spectra from Output Auto spectra

Input Auto spectra or PSDs are calculated from **Output** Auto spectra or PSDs and **FRFs** using the formula,

$$[\{F(\omega)\}\{F(\omega)\}^t] = [T(\omega)]\,[\{X(\omega)\}\{X(\omega)\}^t]\,[T(\omega)]^t$$

$[\{F(\omega)\}\{F(\omega)\}^t]$ ➔ Input Auto spectrum matrix (**m by m**)

$[T(\omega)]$ ➔ $[[H(\omega)]^t[H(\omega)]]^{-1}[H(\omega)]^t$ (**m by n**) matrix

$[H(\omega)]$ ➔ **FRF** matrix (**n by m**)

$[\{X(\omega)\}\{X(\omega)\}^t]$ ➔ Output Auto spectrum matrix (**n by n**)

m ➔ number of Inputs

n ➔ number of Outputs

ω ➔ frequency variable (radians per second)

t ➔ denotes transposed conjugate

-1 ➔ denotes matrix inverse

- ***Only the diagonal elements*** of the **Output** Auto spectrum matrix are used for this calculation

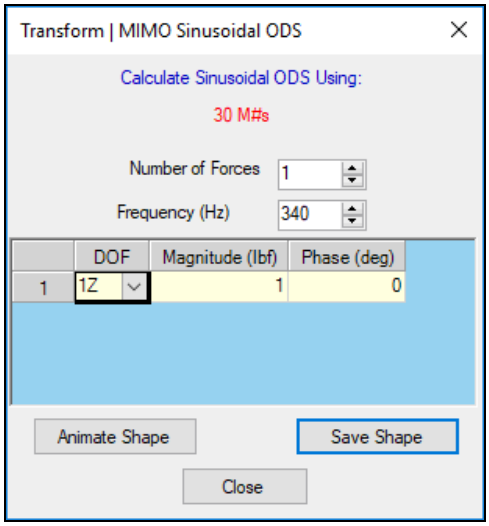
Transform | Sinusoidal ODS

Calculates a ***single frequency* ODS *from multiple sinusoidal*** excitation forces.

The Sinusoidal **ODS** can be ***saved*** in a Shape Table (**SHP**) or ***displayed in animation*** in a ***connected*** Structure (**STR**) window.

- The **ODS** is calculated by multiplying **FRFs** by the **DFTs** of excitation forces at a single frequency.
- Forces can be ***applied at any* Reference DOF** of the **FRFs**
- Each force is defined by its **magnitude & phase**, and the **Reference DOF** at which it is applied to the structure
- The **DOFs** of the Sinusoidal **ODS** are determined from the **Roving DOFs** of the **FRFs**

When this command is executed, the following dialog box is opened.



Animating the Sinusoidal ODS

- ***Press*** the **Animate Shape** button to display the Sinusoidal **ODS** in animation on the structure model in a ***connected*** Structure (**STR**) window

The **M# Links** in the ***connected*** structure ***must be compatible with the M#s*** of the Sinusoidal **ODS** in order to display it in animation. To ensure that the Sinusoidal **ODS** will deflect the structure model correctly,

- ***Press* Save Shape** to save the **ODS** into a Shape Table (**SHP**)
- Execute **M# Links | Create M# Links** from the ***connected*** Structure (**STR**) window to create **new M# Links** to the Sinusoidal **ODS** into a Shape Table (**SHP**)

Acoustic Surfaces

An Acoustic Surface is a special type of Substructure that is used to display acoustic data in a Structure (**STR**) window.

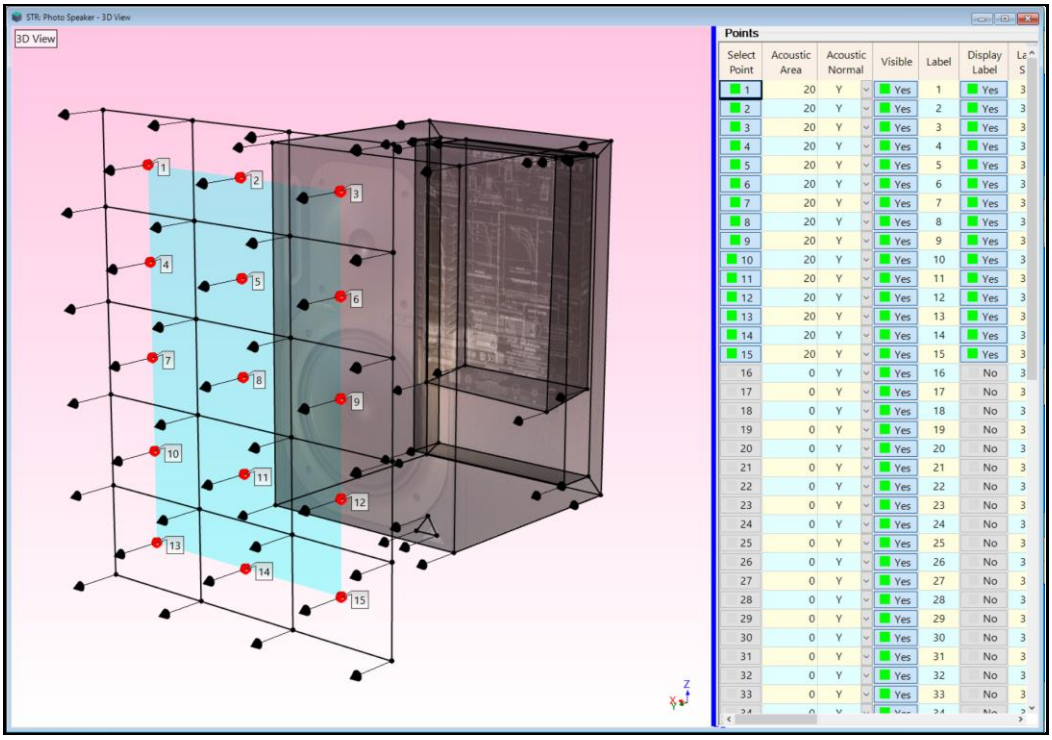
Acoustic data is typically taken on a grid of spatial Points in the vicinity of one or more noise sources.

- **SPL**, **Sound Power** & **Acoustic Intensity** is typically displayed on an Acoustic surface
- Acoustic surfaces are easily created by using the **Drawing Assistant** in the Structure (**STR**) window
- Each measurement Point on an acoustic surface ***is surrounded by an area*** that is determined when the surface is created.

The **Acoustic area** surrounding a Point and the **Acoustic Normal** to the Point are used to calculate **Sound Power** through the surface from **Intensity** data

- **Acoustic area & normal** are calculated when an acoustic surface is created in the Drawing Assistant

- **Acoustic area & normal** are listed in the **Points** spreadsheet and must be edited if the Point coordinates are changed.
- **Acoustic area** is displayed in the **Acoustic Area** column of the **Points** spreadsheet.
- The **Acoustic normal *vector*** (in the Global X, Y, Z direction) is defined in the **Acoustic Normal** column of the **Points** spreadsheet.
- Each of the bold red Points in the figure above is surrounded by 4 Points which define its **Acoustic area.**

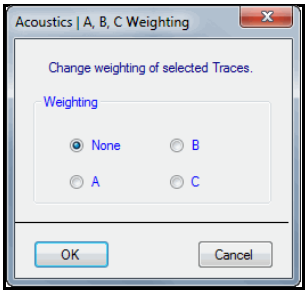


Acoustic Surface Showing Areas & Normal Vectors.

Data Block (BLK) Acoustics Menu

Acoustics | ABC Weighting

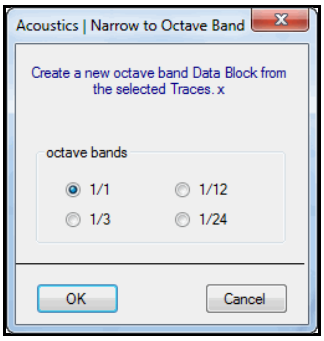
Applies A, B or C weighting to ***all*** (or ***selected***) ***frequency domain measurements*** in a Data Block (**BLK**). When it is executed, a dialog box is opened.



- Choose the type of weighting to be applied and ***click*** on **OK** to apply the weighting

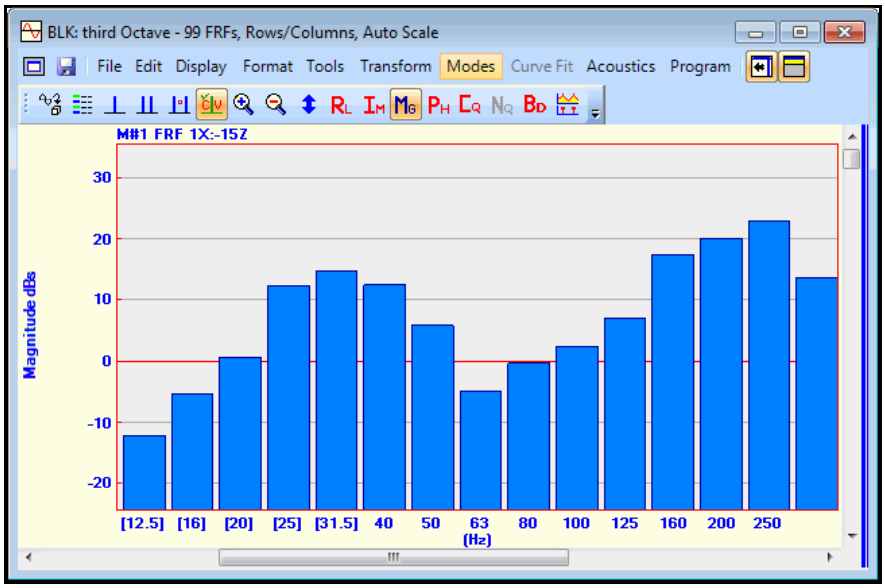
Acoustics | Narrow to Octave Band

Creates a new Data Block (**BLK**) of ***octave band measurements*** from a Data Block (**BLK**) of ***narrow band frequency domain measurements***. When it is executed, a dialog box is opened.



- Choose the octave band in the dialog box and ***click*** on **OK**.

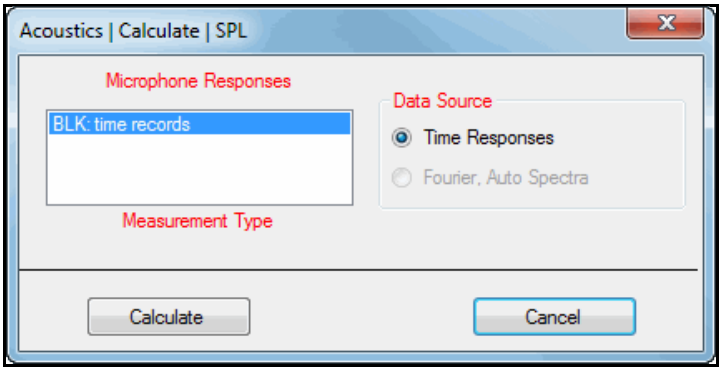
If ***less than 5 samples*** of narrow band data were used to create an octave band, the octave band frequency is enclosed in **brackets [ ]**. In the figure below, several Octave bands were created with ***less than 5 samples***.



Octave Band Measurement Showing Bands Created from Less Than 5 Samples.

Acoustics | Calculate | SPL

Creates a new Data Block (**BLK**) of **Sound Pressure Level (SPL)** measurements from microphone **TWFs**, **DFTs** or Auto spectra. When this command is executed, the following dialog box will open.



Time Responses

If **Time Responses** is chosen as the **Data Source**, all open Data Blocks (**BLK**s) **with TWFs** in them are listed in the dialog box.

DFTs and Auto Spectra

If **Fourier, Auto Spectra** is chosen as the **Data Source**, all open Data Blocks (**BLK**s) with **Fourier spectra** (**DFTs**) or **Auto spectra** in them are listed in the dialog box.

SPL spectra are calculated in the following ways,

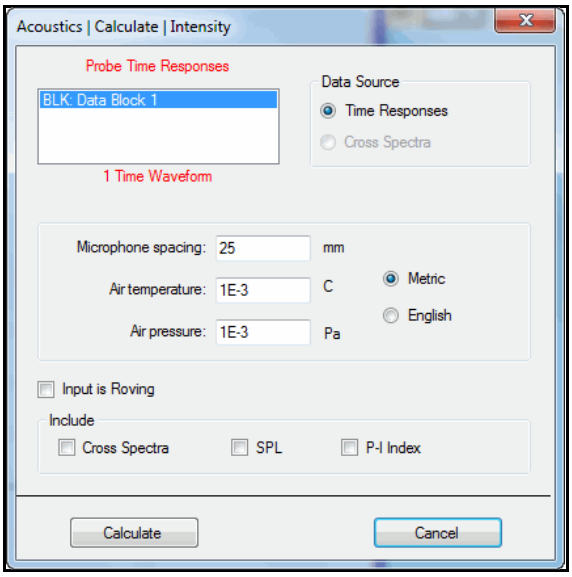
- **DFT *magnitude*** ➔ **SPL** spectrum
- ***Square root*** of an Auto spectrum with ***power units*** ➔ **SPL** spectrum
- Auto spectrum with ***linear units*** ➔ **SPL** spectrum

Acoustics | Calculate | Intensity

Creates a new Data Block (**BLK**) of Acoustic Intensity measurements **from TWFs** or a **Cross spectrum** calculated from data acquired with a **two**-microphone Acoustic Probe.

- Four-microphone data (taken with 3 Responses & 1 Reference) can also be used with this command

When this command is executed, a dialog box is opened



Time Responses

If **Time Responses** is chosen as the **Data Source**, all open Data Blocks (**BLK**s) **with TWFs** in them are listed in the dialog box.

- **Roving waveforms** must be identified as (**Output** or **Both**) in the **Input Output** column of the **M#s** spreadsheet
- **Fixed Reference waveforms** must be identified as (**Input** or **Both***)* in the **Input Output** column of the **M#s** spreadsheet

Cross Spectra

If **Cross Spectra** is chosen as the **Data Source**, all the open Data Blocks (**BLK**s) **with Cross spectra** in them are listed in the dialog box.

Acoustic Intensity is calculated from the Cross spectrum between a pair of microphone responses with the formula,

$$\text{Intensity} = \frac{-(\text{Imaginary Part}(\text{XPS}))}{\rho \Delta X \omega}$$

XPS = Cross Power Spectrum

ρ = Air Density

ΔX = Microphone Spacing

ω = Frequency

- Air density is calculated from the air pressure and temperature values

SPL and P-I Index

Both **SPL** and **P-I Index** measurements can be calculated at the ***same time as*** **Acoustic Intensity** by ***checking*** these selections in the **Calculate Intensity** dialog box.

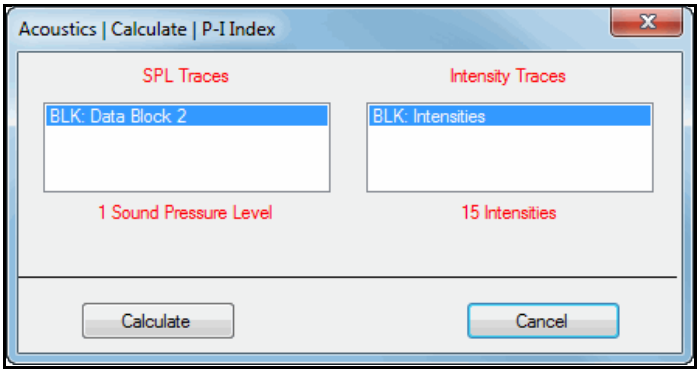
Acoustics | Calculate | P-I Index

Calculates the **Pressure-Intensity (P-I) Index** from SPL and Intensity functions.

The P-I Index is calculated as,

P-I Index (dB) = (SPL (dB Reference 20 ω PA) - Intensity (dB Reference (e-12 watts/m^2))

When this command is executed, a dialog box is opened



- When the **Calculate** button is ***pressed***, a new Data Block (**BLK**) file with **P-I Index M#s** is created

Acoustics | Intensity to Power

Calculates **Sound Power M#s** from a Data Block (**BLK**) containing **Acoustic Intensity M#s**.

Sound Power is calculated by ***multiplying*** **Acoustic Intensity** by the **surface area** surrounding its corresponding measurement Point on an Acoustic Surface in a ***connected*** Structure (**STR**) window.

- The ***connected*** Structure (**STR**) window must have an Acoustic Surface with ***uniquely numbered*** **Points** that match the Point numbers in the **Roving DOFs** of the Intensity measurements
  - ***Each matching*** **Point** must also have a **non-zero** surface area associated with it
- The calculated **Sound Power M#s** are ***added*** to the **Acoustic Intensity M#s** in the same Data Block (**BLK**)

Animating Sound Power & Intensity Together

Sound Power and Acoustic Intensity shapes must be scaled differently in order to display them together in animation. This is done by ***defining two Groups*** of **M#s**

- Execute **Edit | Select M#s | Select By** and choose **Sound Power** from the Measurement Type drop-down list
  - ***Press*** the **Select button** to ***select*** the **Sound Power M#s** and press ***Close***
- ***Double click*** on the **Group** column heading in the **M#s** spreadsheet, and type ***"Sound Power"*** into the dialog box
- Execute **Edit | Select M#s | Select By** again, and choose **Intensity** from the Measurement Type drop-down list, and.
  - ***Press*** the **Select** button to ***select*** the Intensity **M#s** and press ***Close***
- ***Double click*** on the **Group** column heading in the **M#s** spreadsheet, and type **"Intensity"** into the dialog box

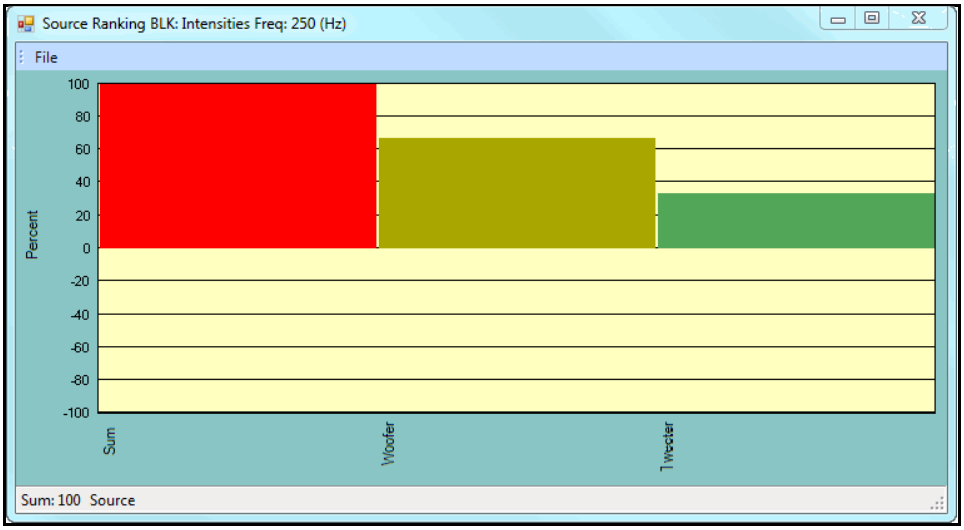
To animate the Sound Power & Acoustic Intensity data together,

- Execute **Deflection | Animate Using | Groups** in the Structure (**STR**) window

Acoustics | Source Ranking | Chart

Opens the Acoustic Source Ranking bar chart window. This window displays a bar chart ranking the relative strengths of the **Acoustic Sources** at the cursor position for ***all*** (or ***selected***) **M#s.**

- In this bar chart, Source ***percentages*** are plotted on the ***vertical axis*** and **Source Names** on the ***horizontal axis***
- Acoustic Sources are defined in the **Acoustic Source** column of the **M#s** spreadsheet



Source Ranking Chart

Values at Cursor Position

The Source Ranking bar chart is updated whenever the Data Block (**BLK**) cursor is moved.

- If the **Line** or **Peak** cursor is displayed, the **M#** values at the cursor position are Source ranked
- If the **Band** cursor is displayed, the ***sum* of the M# values** in the band are Source ranked
- The first bar is the ***Sum*** of all sources and is always **100%**

Which Magnitudes Are Ranked?

- If the **Real** part of the data is displayed, the ***absolute values*** of the **Real** parts are ranked

- If the **Imaginary** part of the data is displayed, the ***absolute values*** of the **Imaginary** parts are ranked
- **Otherwise,** the ***magnitudes*** of the data are ranked

Status Bar

- ***Hover*** the mouse pointer over the Source Rank **bar** of a source to display information for that source on the Status Bar at the bottom of the window

Source Ranking

Measurements are associated with an acoustic source by giving them a common **Acoustic Source** name. An acoustic source would typically be a physical source which is nearest to the Points associated with a group of **M#s**

- Source ranking ***sums the data*** from all Points associated with each Acoustic Source
- After each Source value is calculated, it is ***normalized*** by the total of the magnitudes of all Sources, yielding a **percentage** value for each Source

Source names are entered as text into the **Acoustic Source** column of the **M#s** spreadsheet. Source ranked data can be,

- Displayed in a bar chart
- Animated on an acoustic surface by executing **Deflection | Animate Using | Acoustic Source** in the ***connected*** Structure (**STR**) window
- Saved in a Shape Table (**SHP**) by executing **Acoustics | Source Ranking | Save Shape by Source**

Naming Acoustic Sources

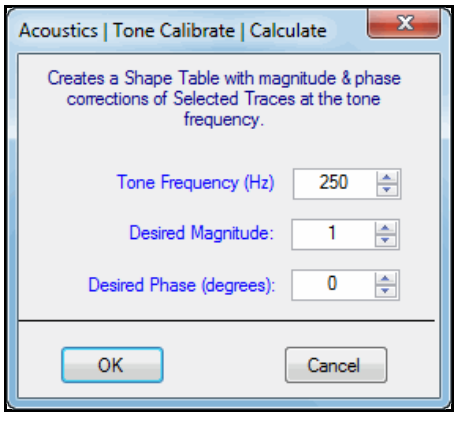
To give the ***same name*** to a group of **M#s linked to Points** on an acoustic surface,

1. Execute **M# Links | Create M# Links** to create **M# Links** in a ***connected*** Structure (**STR**) window containing the structure model with **acoustic surfaces**
2. ***Select*** a **Substructure** on the model that defines ***a single*** **Acoustic Source**
3. Execute **M# Links | Select Source M#s** to select the **M#s** in the Data Block (**BLK**) that are linked to the Source
4. ***Double click*** on the **Acoustic Source** column in the **M#s** spreadsheet
5. Enter an Acoustic Source **name** into the **Acoustic Source** column in the **M#s** spreadsheet

Repeat the above steps to name other Acoustic Sources

Acoustics | Tone Calibration | Calculate

Creates a Shape Table (**SHP**) of scale factors that can be used to calibrate acoustic measurements. When this command is executed, a dialog box is opened.



- Enter the **Tone Frequency**, **Desired Magnitude**, & **Desired Phase** into the dialog box, and ***click*** on OK

Acoustics | Tone Calibration | Apply

Applies the tone calibration scale factors stored in a Shape Table (**SHP**) to the acoustic **M#s** in a Data Block (**BLK**).

- The scale factor for ***each*** **M#** in the **M#s** spreadsheet in the Shape Table (**SHP**) is applied to the **M#** with ***matching*** **DOF** in the Data Block (**BLK**)

Acoustics | Save Ln

Calculates **Ln** values for ***all*** (or ***selected***) **M#s** in a Data Block (**BLK**) and stores them in a Shape Table (**SHP**).

Because noise levels often fluctuate over a wide range and over time, a single value descriptor called the **Leq - Equivalent Level** is often used to characterize the noise level statistics of a signal.

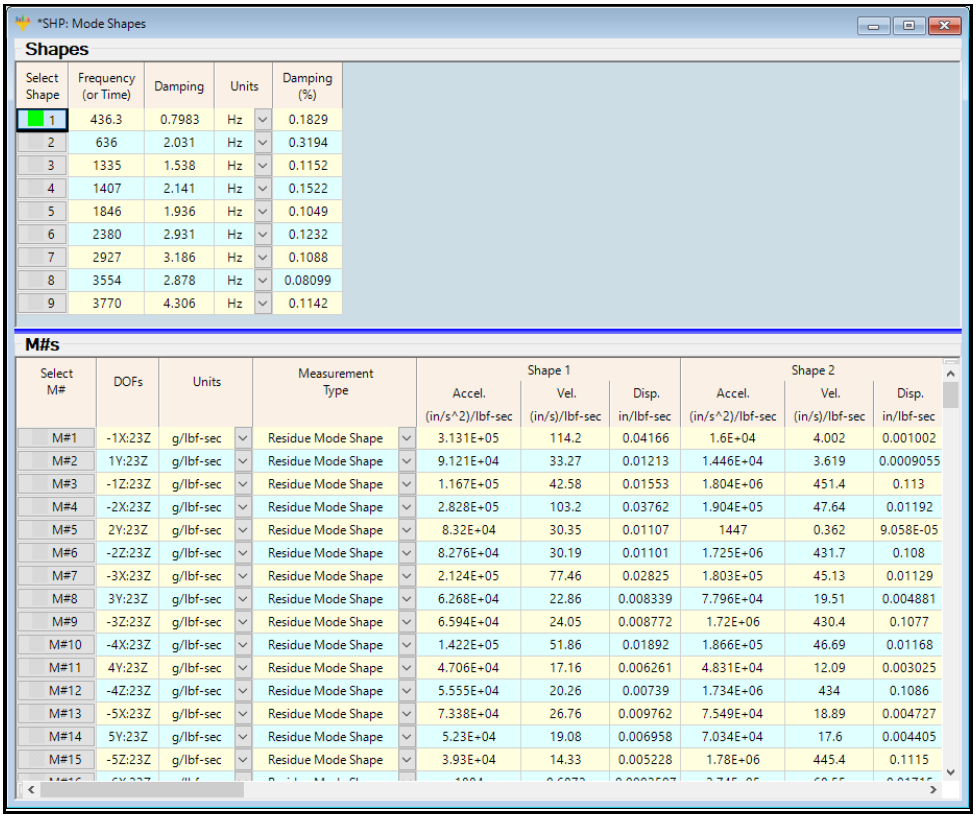
A useful set of **Statistical Noise Levels** are the **Ln** values of an acoustic signal. Any statistical value between 0.01% and 99.99% can be calculated, but the widely used ones are L10, L90 & L95.

- If the **Line** or **Peak** cursor is displayed, **Ln** values are calculated at the **Line** cursor position
- If the **Band** is displayed, **Ln** values are calculated using all the samples in the band

Shape Table (SHP) Display | M#s Menu

Display | M#s | Accel, Vel, Disp

Displays the shape data in the **M#s** spreadsheet in Acceleration, Velocity or Displacement units.



Acceleration, Velocity or Displacement calculations is based on the **Units** of the **M#s.**

If the **Units** are ***acceleration*** units.

- **Velocity** shapes are calculated by ***dividing each shape component by the shape frequency***
- **Displacement** shapes are calculated by ***dividing each shape component by the shape frequency squared***

If the **Units** are ***velocity units***,

- **Acceleration** shapes are calculated by ***multiplying each shape component by the shape frequency***
- **Displacement** shapes are calculated by ***dividing each shape component by the shape frequency***

If the output **Units** are ***displacement***,

- **Velocity** shapes are calculated by ***multiplying each shape component by the shape frequency***
- **Acceleration** shapes are calculated by ***multiplying each shape component by the shape frequency squared***

Shape Table (SHP) Tools Menu

Tools | Integrate

Integrates **Residue mode shapes** from ***acceleration to velocity*** units or from ***velocity to displacement*** units.

- The mode shapes must be converted to **Residue mode shapes** before using this command
- Integration is performed by ***dividing each shape component*** by its ***complex pole*** (***frequency & damping***)

Tools | Differentiate

Differentiates **Residue mode shapes** from ***displacement to velocity*** units or from ***velocity to acceleration*** units

- The mode shapes must be converted to **Residue mode shapes** before using this command
- Differentiation is performed by ***multiplying each shape component*** by its ***complex pole*** (**frequency & damping**)

Tools | Shape Product

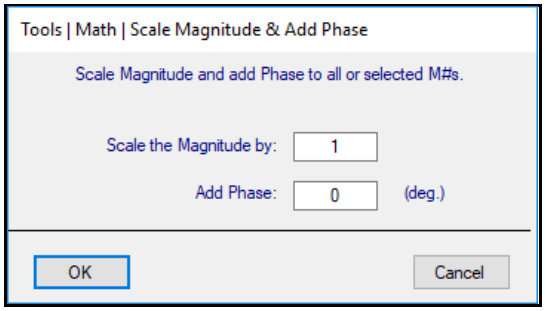
Multiplies ***all*** (or ***selected***) shapes together.

- A Shape Product shows ***where all shapes have node lines*** (zero values), and hence where ***inactive*** **DOFs** are located
- A Shape Product shows ***where all shapes have anti-nodes*** (large magnitudes**)**, and hence where ***active*** **DOFs** are located

When a Shape Product is displayed in animation on the structure model in a ***connected*** Structure (**STR**) window, ***node lines*** and ***anti-nodes are easily seen***

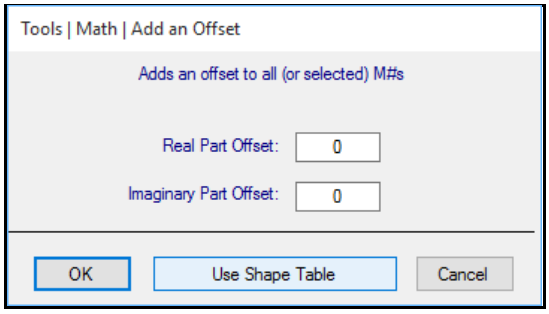
Tools | Math | Scale M#s

Scales the ***magnitude*** and ***adds phase*** to ***all*** (or ***selected***) Shapes and ***all*** (or ***selected***) **M#s**.



Tools | Math | Add an Offset

Adds a complex (real & imaginary) offset to ***all*** (or ***selected***) Shapes and ***all*** (or ***selected***) **M#s**.



Tools | Math | Invert M#s

Replaces each **M#** with its ***inverse*** for ***all*** (or ***selected***) Shapes and ***all*** (or ***selected***) **M#s**.

Tools | Math | Square M#s

Replaces each **M#** with its ***value squared*** for ***all*** (or ***selected***) Shapes and ***all*** (or ***selected***) **M#s**.

Tools | Math | Square Root of M#s

Replaces each **M#** with the ***square root*** of its value for ***all*** (or ***selected***) Shapes and ***all*** (or ***selected***) **M#s**.

Tools | Math | Add (Subtract, Multiply, Divide) two M#s

Performs the indicated operation between **M#s** in a Shape Table (**SHP**) and ***a selected*** **M#** in the same or a different Shape Table (**SHP**).

- If two Shape Tables (**SHP**s) have the ***same number of M#s*** in them, you can choose to perform the operation ***between M# pairs*** in the two Shape Tables (**SHP**s)